

ABSTRACT

INVESTIGATION OF BEARING CAPACITY  
OF THIN WALL RIBBED REINFORCED  
CONCRETE PANELS

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Full scale tests were undertaken to determine the bearing capacity of thin wall ribbed reinforced concrete panels, since not enough research data is available to provide adequate information concerning the strength of such panels. Five full scale panels, with variable reinforcement, were tested as bearing walls under axial and eccentric loading. Deflections, crack appearance and propagation under increasing load, the behavior at junctions of thin walls, with ribs, and the ultimate capacity were recorded and analysed.

Results obtained were compared with calculated values based on present ACI design practice, with the purpose of determining if the empirical ACI design method, developed for solid walls, is also applicable for thin wall ribbed panels. (1). Results show that the ACI design method is applicable in evaluating bearing capacity of thin wall panels.

ACKNOWLEDGEMENTS

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NOTATIONS

## NOTATIONS

$a$	Depth of equivalent rectangular stress block
$A_g$	Gross cross-sectional area
$A_s$	Area of steel reinforcement
$B_1$	ax, factor
$\epsilon_s$	strain in steel, in/in
$E_s$	modulus of Elasticity of Reinforcement
$f'_c$	Ultimate compressive strength of concrete, psi
$FC_1$	Compressive force due to concrete in slab
$FC_2$	Compressive force due to concrete in rib
$Fs_1$	Compressive force due to rib reinforcement
$Fs_2$	Compressive force due to slab reinforcement
$F_y$	Yield strength of reinforcement
$h$	Overall thickness of the wall
$l_c$	Vertical distance between supports
$m$	$f_y/f'_c$ yield strength ratio of steel to concrete
$n$	$E_s/E_c$ modular ratio
$P_u$	Failure load of test panels
$P_f$	Factored axial load strength of wall
$P_u$	Nominal axial load strength of wall.
$p_m$	Ratio of yielded reinforcement area to gross area
$p_n$	Ratio of non-yielded reinforcement area to gross area.
$x$	Distance from extreme compressive fibre to neutral axis.
$\phi$	Strength reduction factor

CHAPTER I  
INTRODUCTION

## INTRODUCTION

Prefabricated, reinforced concrete panels have recently become more widely used in building industry for housing construction. Present technology enables the making of relatively thin panels. The required rigidity is provided with perimeter ribs. Such panels introduce economy in consumption of materials and have been applied for example, by Zielinski for walls and roofs for low cost housing construction. (2), (3). Such panels have been for a number of years a subject of research at Concordia University. Earlier tests were done on similar panels working as ribbed floor elements or wall beam system. (4), (5).

The main purpose of the present research is to study the behavior and strength of thin wall panels working as bearing wall elements. Not much data is available in this respect since most of previous research work on behavior and bearing strength was done on solid (thick) wall panels. (6), (7).

CHAPTER 2  
RESEARCH PROGRAM

## RESEARCH PROGRAM

### 2.1 DESCRIPTION OF TEST PANELS

The dimensions and reinforcement details of panels are shown in Figs. 2.2 - 2.7. The panels have a very thin 1 1/2 in. concrete slab reinforced with a wire mesh. The rigidity of the panels is provided by the 8 in. deep 2 1/2 in wide rib, which is reinforced with longitudinal bars and ties. The overall dimensions of the panels are 48 in. x 108 in. Some panels had additional cross ribs.

All panels have edge ribs formed in such a way that when placed side by side with in-situ placed grout a shear key joint is created. The panels may also be provided with inserts for welded connections. Additional strength in connection may be created by protruding main flexural reinforcement to the outside of the panels and into the cast in situ concrete in joists.

More detailed description of individual panels tested is given below.

Panel 168-9 (H1), was similar to panel 168-8. Also here a combination of wire meshes was used, a 6x6 - 6/6 over the entire length of the slab and a heavier mesh of 6x6 - 1/1 in the shorter support segment. Bars 1#3 and 1#4 were used in the upper longitudinal rib, 1#6 and 1#8 in the lower one. The ties provided were 5#4 in all ribs.



Panel 168-11 (H2); comparable to panel 168-9, contained a 6x6 - 10/10 wire mesh over the entire length of the membrane and a 6x6 - 1/1 mesh at mid height. Bars 1#6 and 1#8 were used as reinforcement of the lower longitudinal rib and 1#3 and 1#4 of the upper rib. This panel also had intermediate ribs similar as in panel 168-10 but reinforced with 1#3 and 1#4 bars.

Reinforcing steel yield strengths  $F_y$  were established by testing of 18 in long samples for every bar of reinforcing bar and wire mesh. Steel test results are shown in Table 2.1.

Panel 168-8 (H3), contained a wire mesh combination of one light wire mesh 146-1210 over the entire length of the slab and an additional mesh 6x6 - 6/6 in the shorter support segment. The lower rib had 2#5 rebars and the upper rib had 1#2 and 1#3 rebars. Both ribs had 2#4 stirrups.

Panel 169-10 (H4), contained reinforcement similar to panel 168-8 but in addition it had two intermediate ribs 6 in. deep and 1#6 and at 5#6 of the panel height. These ribs were reinforced with 1#2 bars each, and were provided for additional rigidity of the membrane or as a frame for a possible window opening.

Panel 168-7 (H5), representing a window panel was the most heavily reinforced. It contained a two 6x6 - 6/6 welded wire fabric wire meshes as slab reinforcement, 2#9 in longitudinal lower rib, 1#3 and 1#4 and 1#6 stirrups in the longitudinal upper rib.

TABLE: 2.1 STEEL STRENGTHS TESTED

REINFORCEMENT TYPE		NOMINAL AREA IN <sup>2</sup>	AVERAGE Fy PSI
MESH 146-1210	GAGE #10	0.0143	85,314.7
	GAGE #12	0.0087	87,314.7
MESH 6x6 - 10/10	GAGE #10	0.0143	83,449.9
MESH 6x6 - 6/6	GAGE #6	0.02895	72,884.3
MESH 6x6 - 11	GAGE #1	0.0629	76,364.6
REBAR	#2	0.05	44,133.4
REBAR	#3	0.11	55,218.2
REBAR	#4	0.20	48,066.7
REBAR	#5	0.31	49,731.2
REBAR	#6	0.44	43,522.7
REBAR	#6	0.44	51,098.8

## 2.2 LOADING SCHEMES

One panel marked H1 was loaded eccentrically and four panels marked H2-H5 were loaded at the center of gravity.

The load was applied by means of a hydraulic jack through a calibrated load cell, a stiffened beam and a 1/4 in. masonite pad. The load was applied in increments controlled by reading of pressure on the monometer and strain indicator from the load cell.

Dial gages were used to measure the horizontal (z-axis) and the vertical (y-axis) displacements. Loading scheme and positions of the dial gages are shown in Figure 2.1.

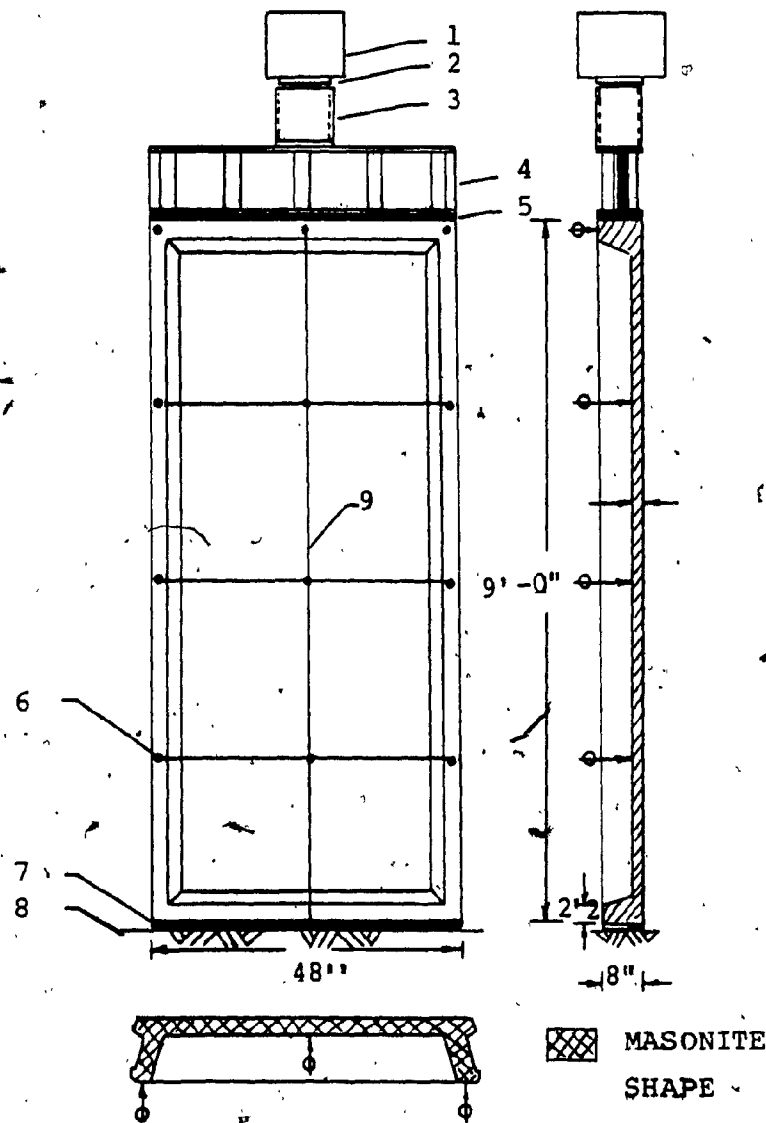
In order to support panels on an area corresponding to panel cross section in the middle a 1/4 in. masonite pad was cut similar to cross section dimensions, as shown in figure 2.1.

The surface of the panels was either brushed clean or painted white for easier crack observation. Rectangular grid lines as seen in Figure 2.1 were drawn on the wall surface so as to facilitate the location and the marking of the cracks during testing.

Readings were taken at each load increment from all the dial gages and strain indicator and the panel was carefully examined for any cracks. In the event that a crack had occurred under the particular load it was visibly marked

along the crack with a marker for further easier observation and photography.

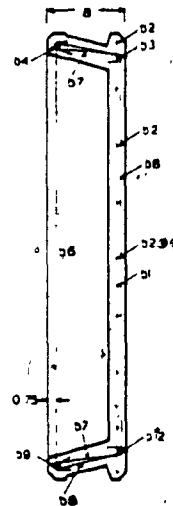
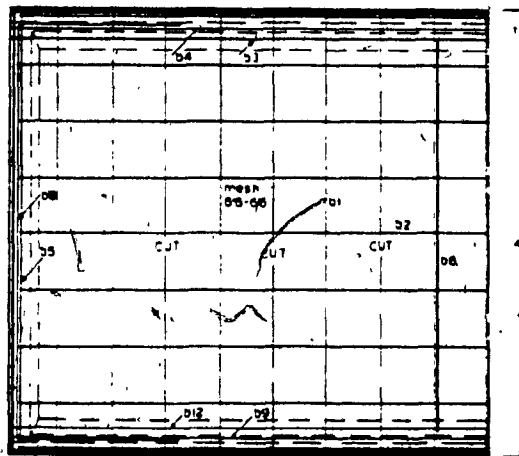
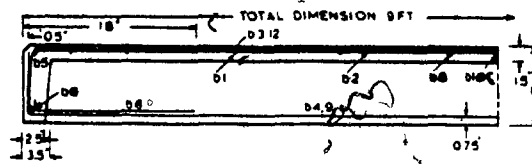
All the panels tested were loaded till failure. Crack patterns were recorded on scaled drawings and sequential photographs were taken. (Appendix C).



TYPICAL CROSS-SECTION

Fig. 2.1 LOADING SCHEME

1. HYDRAULIC JACK
2. 6" PISTON
3. LOAD CELL.
4. RIDGE BEAM.
5. MASONITE PAD
6. DIAL GAGES.
7. MASONITE PAD & MORTAR
8. RIGID FLOOR.
9. GRID LINES



## 4.2: Example of Test Panel

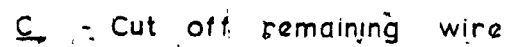
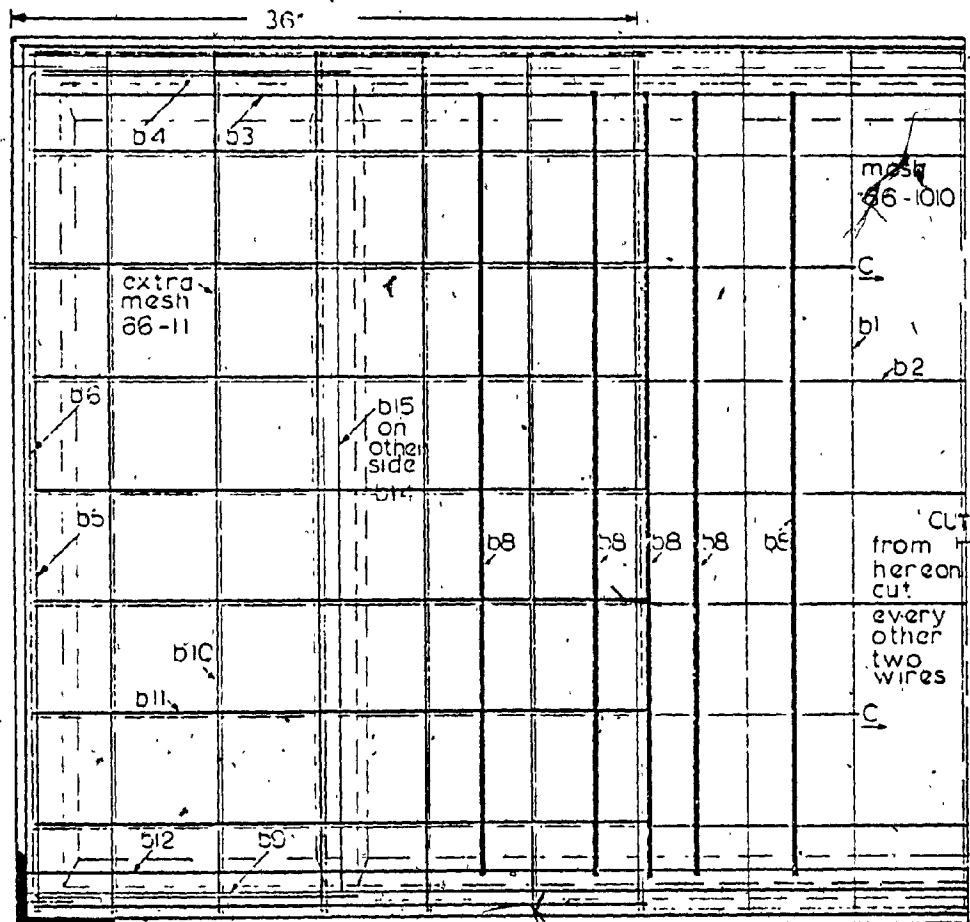


Figure 2.3  
Details of Reinforcement Panel 168-9 (H1)

REINFORCEMENT TYPE 168-9				
BAR NO	TYPE & SIZE OF BARS	NO OF BARS	LENGTH OF BAR, in	F <sub>y</sub> ksi
b1	MESH 6x6 - 6/6	17 cut 6	46.25	
b2		9 cut 3	122.5	
b3	*3	1	122.5	40
b4	*4	1	119.5	40
b5	*2	2	46.25	40
b6	*2	2	82.25	40
b7	*2	38	10.75	40
b8	*4	5	65.25	40
b9	*8	1	108	60
b10	EXTRA MESH 6x6 - 1/1	6 cut 2	134	
b11		9 cut 1	35.5	
b12	*6	1	108	40

Figure 2.3a  
Details of Reinforcement Panel 168-9 (H1)



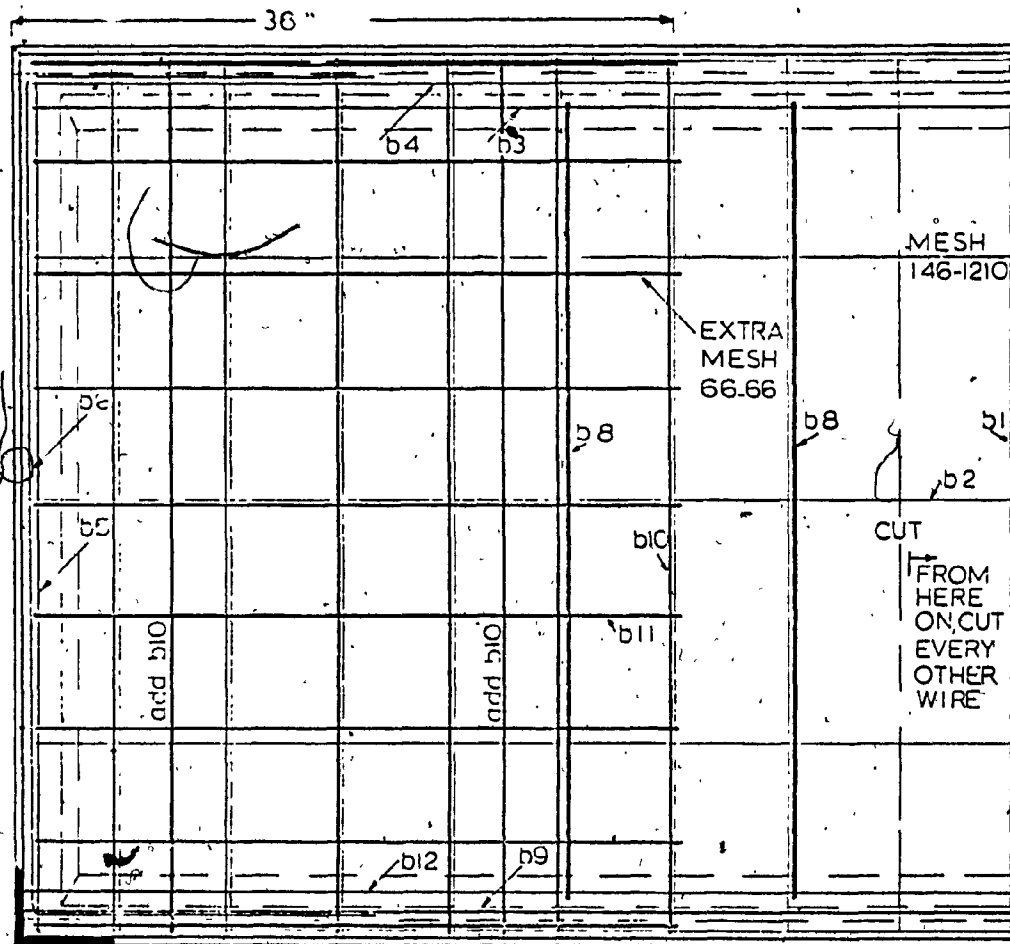


CUT - WHOLE WIRE TO BE CUT OFF  
C - CUT OFF REMAINING WIRE

Figure 2.4  
Details of Reinforcement Panel 168-11 (H2)

BAR NO	TYPE & SIZE OF BARS	NO OF BARS	LENGTH OF BAR, in.	F <sub>y</sub> ksi.
b1	mesh	17	46.25	
b2	66-1010	9	122.5	
b3	*3	1	122.5	40
b4	*4	1	119.5	40
b5	*2	2	46.25	40
b6	*2	2	82.25	40
b7	*2	2	107.5	40
b8	*4	5	65.25	40
b9	*8	1	108	60
b10	mesh	6	134	
b11	66-11	9	35.5	
b12	*5	1	108	60
b14 b15	*3 rhs rib *4 lhs rib	1	56.75	40

Figure 2.4a  
Details of Reinforcement Panel 168-11 (H2)

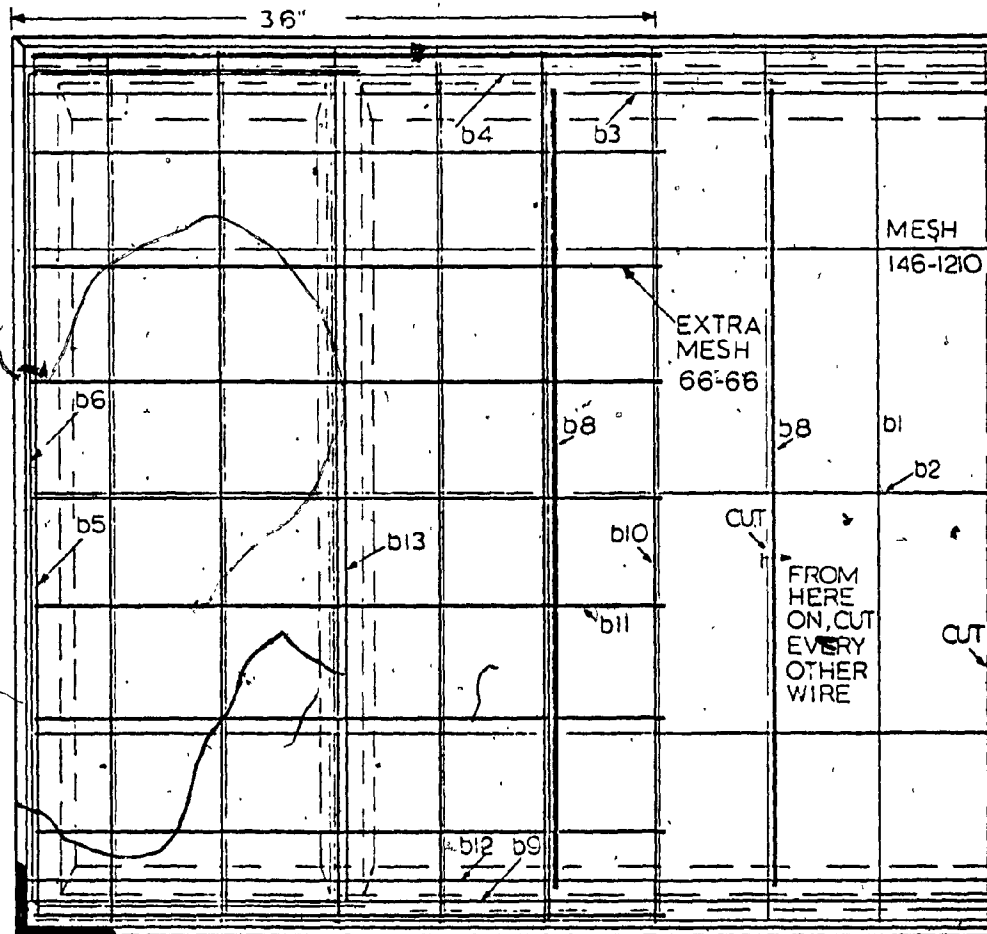


CUT- WHOLE WIRE TO BE CUT OFF

Figure 2.5  
Details of Reinforcement Panel 168-8 (H3)

BAR NO	TYPE & SIZE OF BARS	NO OF BARS	LENGTH OF BAR, in	F <sub>y</sub> ksi.
b1	mesh	17 cut 5	46.25	
b2	146-1210	5	122.5	
b3	*2	1	122.5	40
b4	*3	1	119.5	40
b5	*2	2	46.25	40
b6	*2	2	82.25	40
b7	*2		107.5	40
b8	*4	2	65.25	40
b9	*5	1	108	60
b10	mesh	6 add 2	134	
b11	66-66	9	35.5	
b12	*5	1	108	60

Figure 2.5a  
Details of Reinforcement Panel 168-8 (H3)

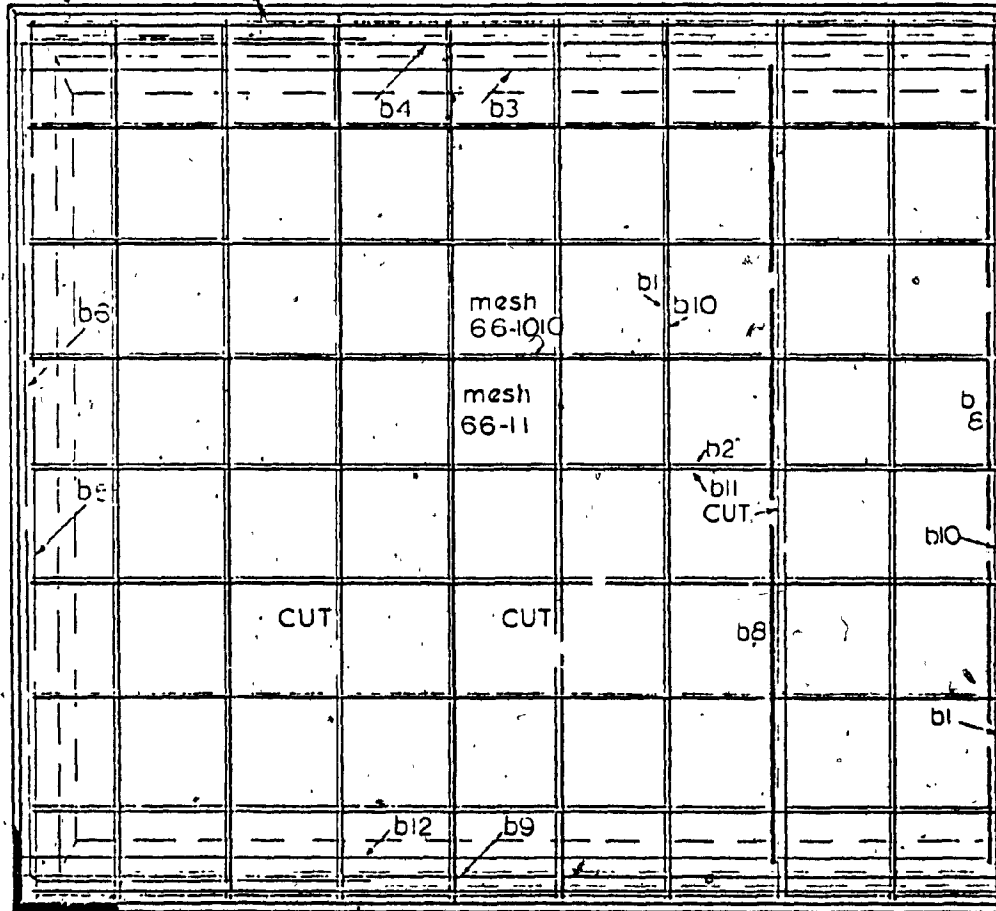


CUT- WHOLE WIRE TO BE CUT OFF

Figure 2.6  
Details of Reinforcement Panel 168-10 (H4)

BAR NO	TYPE & SIZE OF BARS	NO OF BARS	LENGTH OF BAR, in	F <sub>y</sub> ksi
b1	mesh 146-1210	17 cut6	46.25	
b2		5	122.5	
b3	*2	1	122.5	40
b4	*3	1	119.5	40
b5	*2	2	46.25	40
b6	*2	2	82.25	40
b7	*2		10.75	40
b8	*4	2	65.25	40
b9	*5	1	108	60
b10	mesh 66-66	6	134	
b11		9	35.5	
b12	*5	1	108	60
b13	*2	2	56.75	40

Figure 2.6a  
Details of Reinforcement Panel 168-10 (H4)



CUT- WHOLE WIRE TO BE CUT OFF

Figure 2.7  
Details of Reinforcement Panel 168-7 (H5)

BAR NO	TYPE & SIZE OF BARS	NO OF BARS	LENGTH OF BAR, in	F <sub>y</sub> ksi.
b1	mesh 66-66	17 cu ft	46.25	
b2		9	122.5	
b3	*3	1	122.5	40
b4	*4	1	119.5	40
b5	*2	2	46.25	40
b6	*2	2	82.25	40
b7	*2	38	107.5	40
b8	*6	3	65.25	60
b9	*9	1	108	60
b10	mesh 66-66	17	46.25	
b11		9	122.5	
b12	*9	1	108	60

Figure 2.7a  
Details of Reinforcement Panel 168-7 (H5)



CHAPTER 3  
TEST OBSERVATIONS, AND RESULTS

## TEST RESULTS

The following observations were made during the tests.

1. Failure loads (Table 3.1)
2. Instant of crack appearance and propagation under increasing load. (Figs.).
3. Displacements in the horizontal (z-axis) and vertical (y-axis) directions Table 3.2 & 3.3.
4. Mode and locations of failure.

### 3.1 Failure Loads

Failure loads and loading schemes of each panel tested are given below.

TABLE 3.1 TEST SCHEDULE AND RECORDED STRENGTHS

TEST NO.	PANEL MARK REINFORCEMENT DETAILS	LOADING SCHEME	$f'_c$ PSI	FAILURE LOAD $P_f$ KIPS
1	168-9 H1	e	5259	200
2	168-11 H2	c	5073	226
3	168-8 H3	c	5306	270
4	168-10 H4	c	4698	275
5	168-7 HS	c	5023	309

e: eccentrically loaded  
c: concentrically loaded

### 3.2 OVERALL BEHAVIOR AND CRACK PROPAGATION

Panel 168-9 (H1), was loaded eccentrically and it failed at a load of 200K. Corresponding to an eccentricity of 2 1/2 in. measured from the center of gravity, it can be estimated that the panel failed at an imposed moment of 41.67 K. ft. First crack occurred at a load of 46K. Longitudinal cracks and separation of the side ribs from the wall membrane occurred at the top quarter of the panel. The panel had some existing shrinkage cracks which kept on widening and extending along. Some horizontal cracks occurred at 114K and 200K.

Panel 168-11 (H2), was concentrically loaded. The failure load was 226 K. Vertical as well as horizontal cracks occurred on the panel. There was a separation of ribs from the wall membrane. The top half part of the panel twisted and inclined on one side a small angle from the vertical. Twisting probably resulted by a weakened rib on this side which was slightly damaged during handling. Separation of the longitudinal ribs from the slab membrane was insignificant compared with panel 168-9, probably because of the presence of cross ribs.

Panel 168-8 (H3), was loaded concentrically. The failure load was 270 K. Most cracks occurred along the perimeter of the slab at junctions with longitudinal ribs. Failure occurred at the top, at the intersection of the rib and the

wall membrane.

Panel 168-10 (H4) loaded concentrically failed 275 K. As panel 168-11, it had two internal cross ribs. At the connection of the cross ribs a few cracks, but no separation along the perimeter ribs occurred. Separation of edge ribs from membrane occurred at failure at the bottom.

Panel 168-7 (H5), was the most heavily reinforced. It had a window opening of 2 ft. x 2 ft. Failure load was 309 K, the highest of all the panels. Cracks were vertical. Failure occurred around the window opening extending up to the edge ribs. There was a change of curvature on one side of the panel.

### 3.3 MODE OF DEFLECTION

Generally maximum deflections occurred at the center of most panels and deformed ~~along~~ single curvature in the direction of wall slab. Panels having internal cross ribs showed smaller deflections both in the horizontal and vertical directions and deformed with double curvature. In all cases panels failed at the intersection of the ribs and the slab at the top or bottom where there was a sudden change of cross section.

### 3.4 GENERAL OBSERVATIONS ON MODE AND LOCATION OF FAILURE

Common to all panels was the fact that all deflected in one direction, outwards in the direction of the wall

membrane. This phenomenon is a result of the unsymmetric channel shape of the cross section. Most failures occurred at junctions of bottom or top ribs with the slab, where the cross section changes and at corners, in areas of concentration of stresses.

Heavier reinforced panels failed at higher loads.

Panels containing internal cross (ribs (stiffening ribs)) developed pronounced separation of cross ribs from the wall membrane and most of the failures occurred around the ribs.

Two such panels tested showed similar horizontal displacements and deformations as can be seen in Figs. 3.4, 3.6-7, 3.10-11.

The window panel developed vertical cracks extending from bearing ribs at the top and bottom to the corners of the window. A combined stress state of compression and tension above and below the window resulted in concrete failure around that area.

The eccentrically loaded panel failed at the lowest load as compared to other panels and demonstrated the largest vertical displacements.

Crack pattern drawings of panels are shown in Figs. 3.14-3.18. The numbers marked on crack patterns represent loads in kips at which cracks were noticed. Dashed lines represent cracks due to shrinkage and handling. Areas of failure are shown by hatched lines.

Photographs of cracked panels are shown in  
Appendix C.

TABLE 3.2: RECORDED HORIZONTAL DISPLACEMENTS AT OR BEFORE FAILURE FOR CENTER POINT.

PANEL MARK	DEFLECTIONS $\times 10^{-3}$ in											
	LEFT SIDE				CENTER				RIGHT SIDE			
	L <sub>1</sub>	L <sub>2</sub>	L <sub>3</sub>	L <sub>4</sub>	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>
168-9 (H1)	431	289	+229	+183	-52	-295	-277	-261	-45	-244	-288	-228
168-11 (H2)	-73	-97	-76	-91	-189	-188	-166	-83	-137	-236	-225	-122
168-8 (H3)	-275	-167	-147	-75	-167	-316	-326	-331	-47	-290	-438	-311
168-10 (H4)	191	264	64	206	142	106	125	41	-10	-31	-15	-89
168-7 (H5)	-264	-218	-237	-156	-237	-292	-269	-143	-277	-174	-104	-26

TABLE 3.3: OVERALL VERTICAL DISPLACEMENTS RECORDED  $\times 10^3$  in.

LOAD MARK	46	69	92	114	137	160	183	206	229	275	309
168-9 H1	179	238	282	317	339	413	<del>385</del>				
168-11 H2	43	53	63	71	79	87	94	103			
168-8 H3	28	44	55	69	78	92	106	120	144		
168-10 H4	20	49	63	77	89	104	111	121	129	140	
168-7 H5	160	180	192	198	203	209	217	224	231	238	244



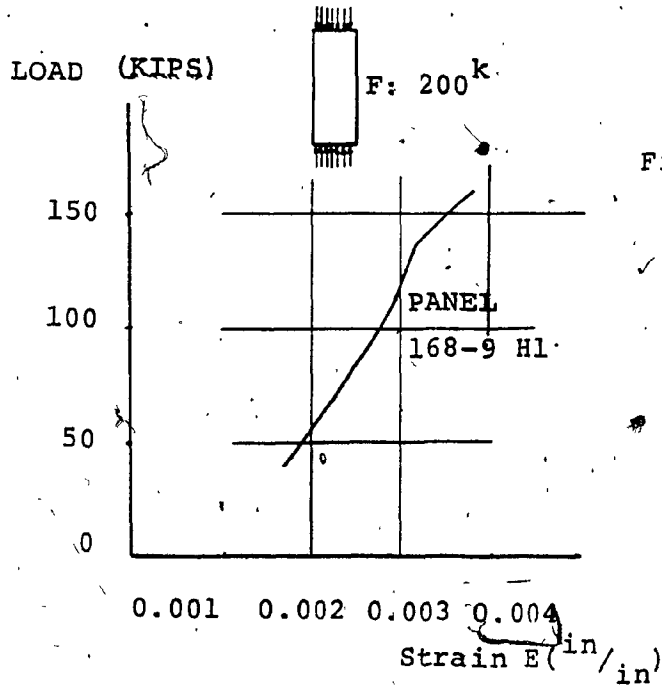
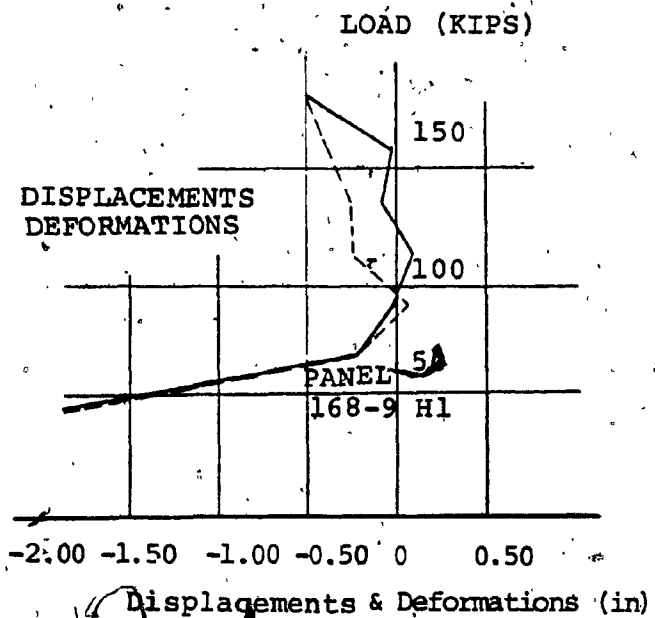


Fig. 3.1: Vertical Displacements of Eccentrically Loaded Panel.

Fig. 3.2 : Horizontal Displacements and Deformations of



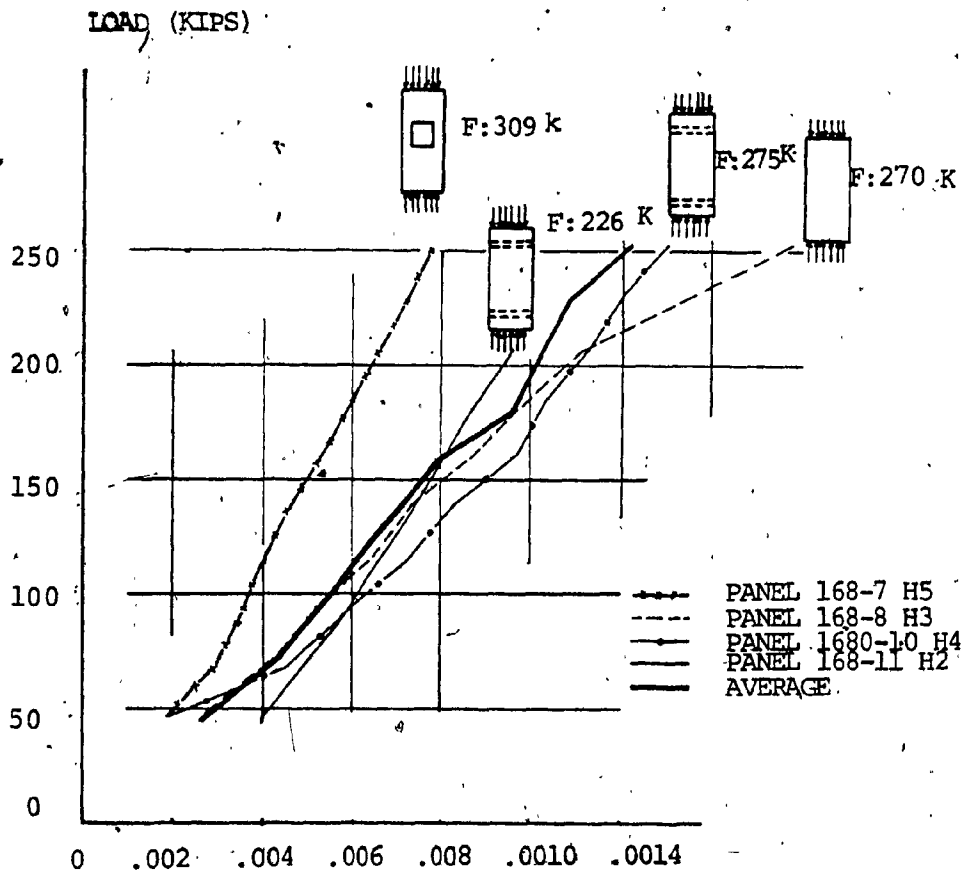
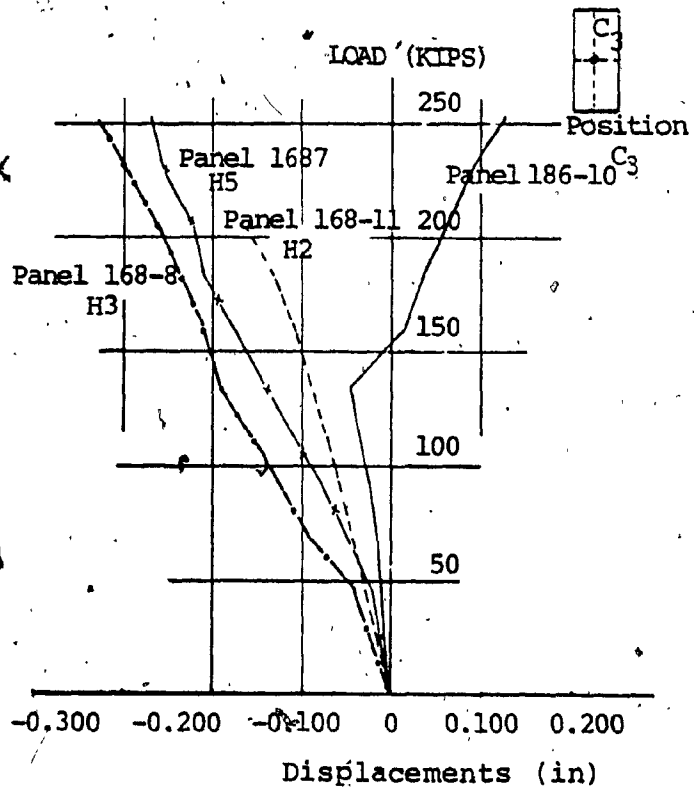


Fig. 3.3

Vertical  
Concentrically loaded  
Panels.

Fig. 3.4

Horizontal  
of Point  $C_3$ .



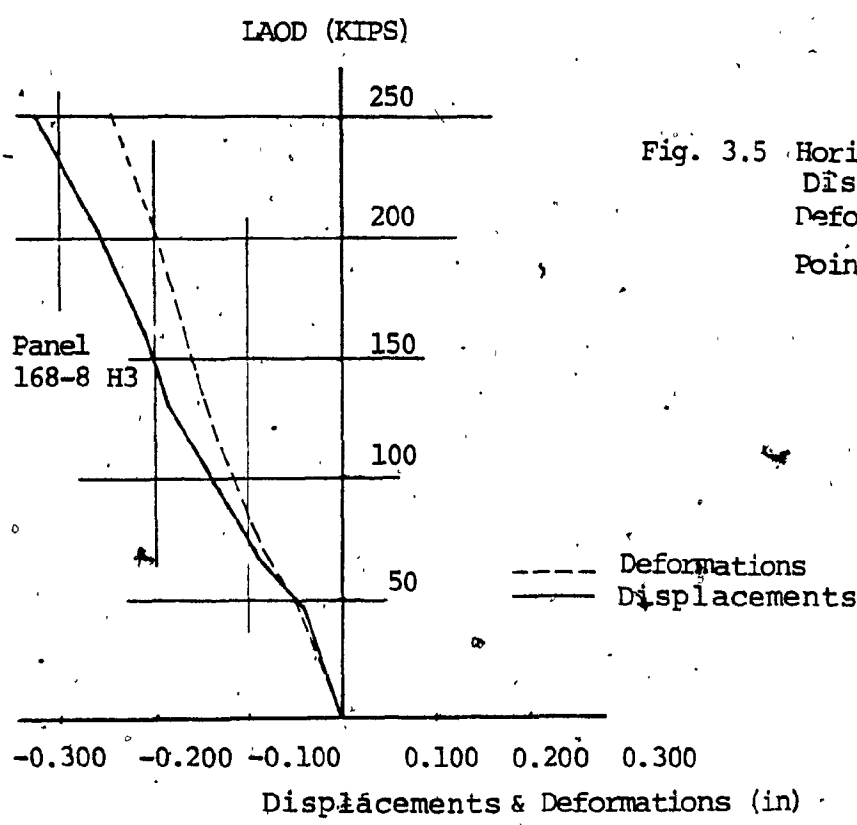
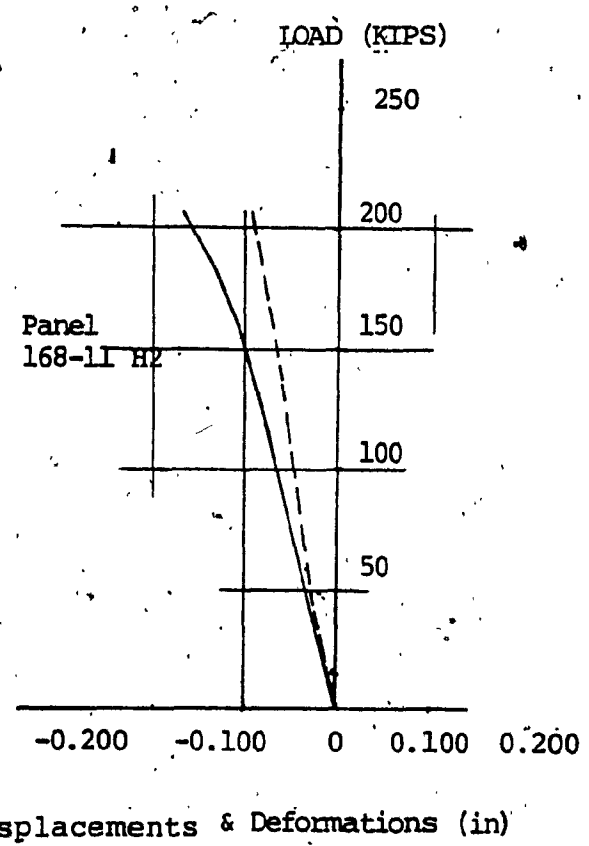


Fig. 3.5 Horizontal Displacements and Deformation of Point  $C_3$ .

Fig. 3.6 Horizontal Displacements Deformation of Point  $C_3$ .



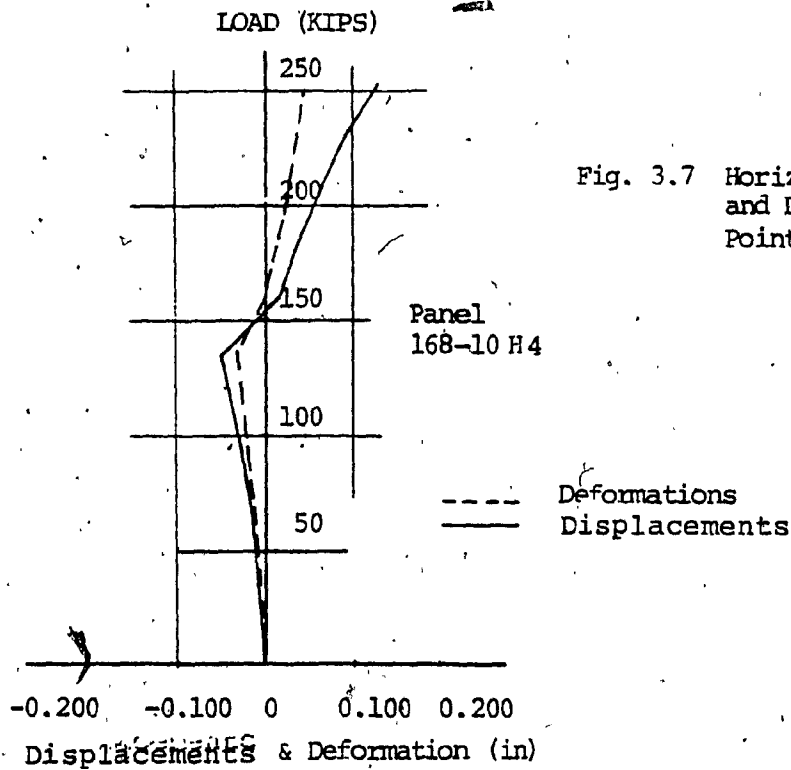
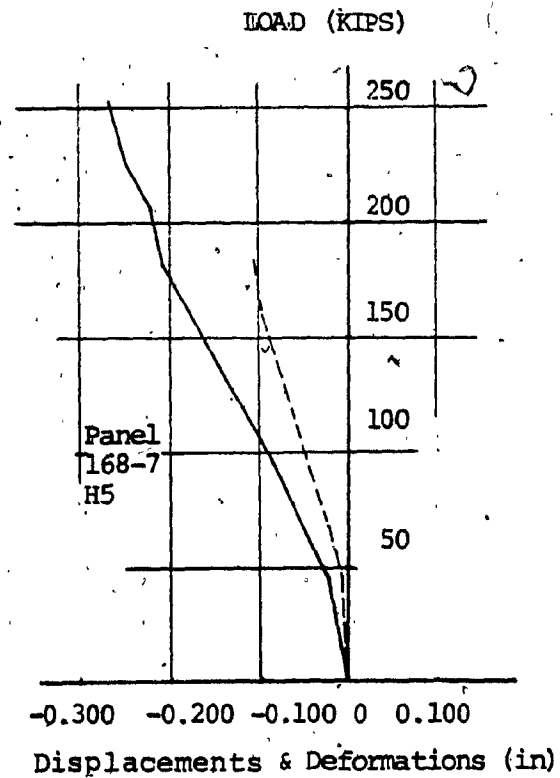


Fig. 3.7 Horizontal Displacements and Deformation of Point  $C_3$ .

Fig. 3.8  
Horizontal Displacements and Deformation of Point  $C_3$



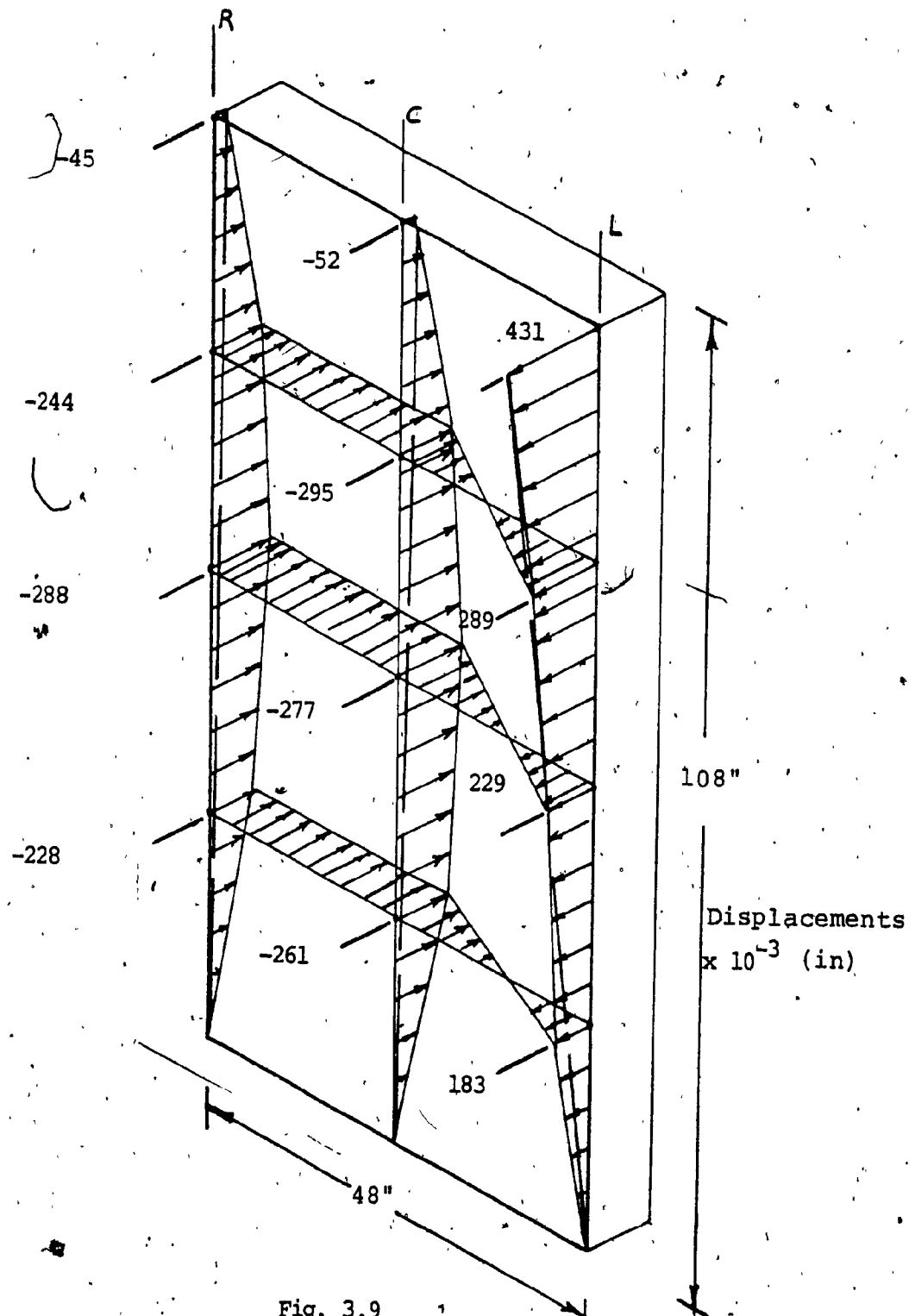


Fig. 3.9

Displacements and deformations Panel 168-9 (H1).

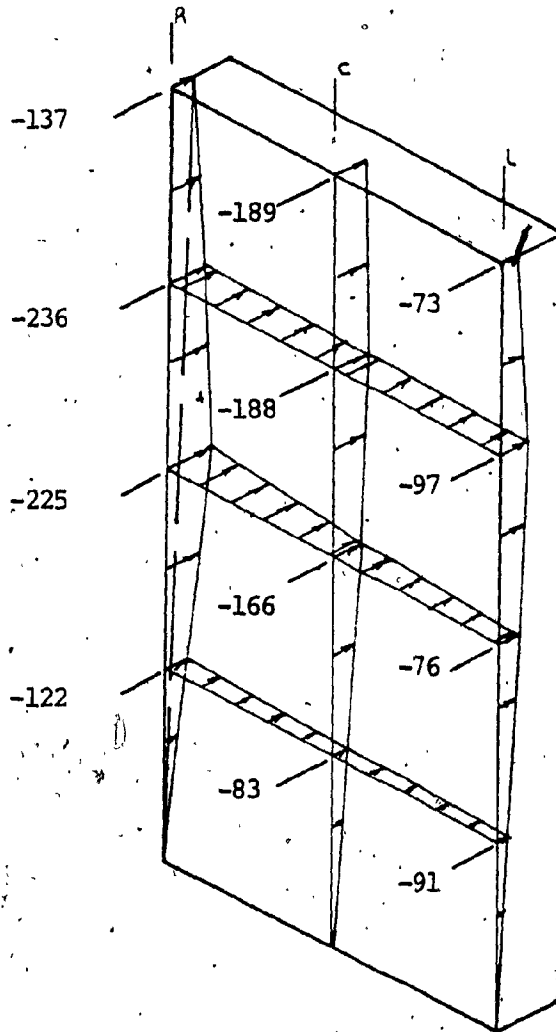


Fig. 3.10 Overall Displacements and deformations Panel 168-9 (H1).

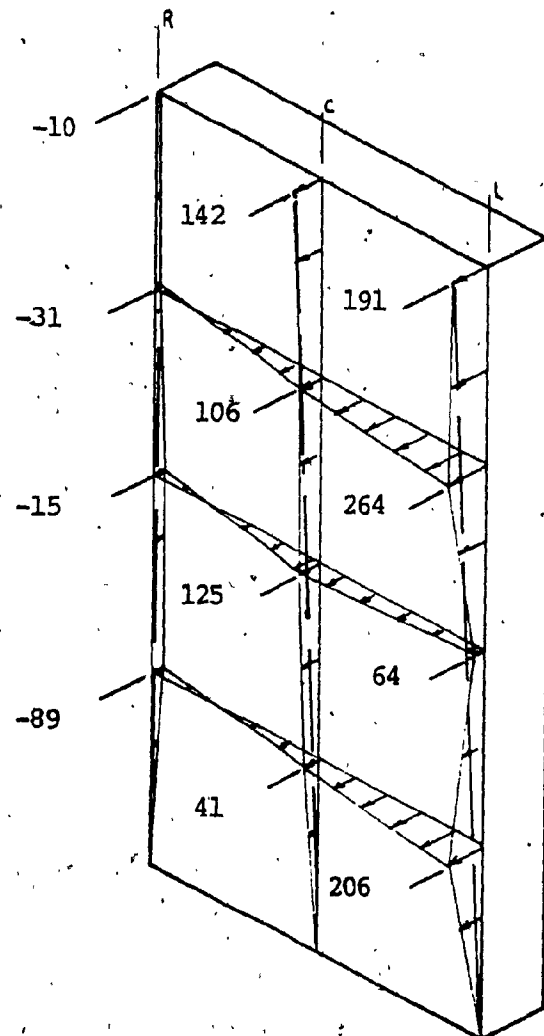


Fig. 3.11

Overall Displacements and deformations Panel 169-9 (H1)

Displacements  $\times 10^{-3}$  (in)

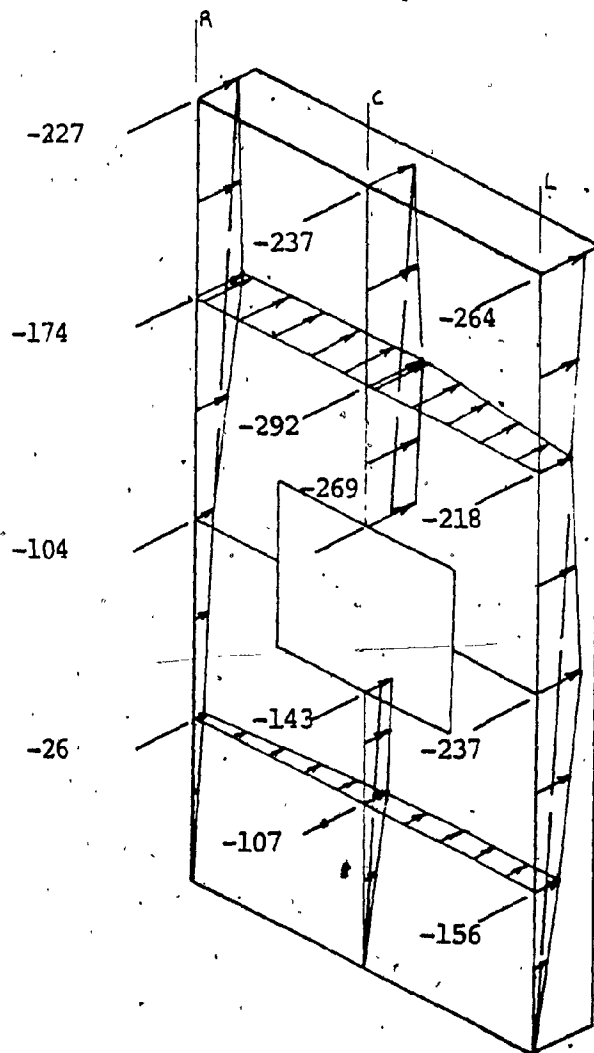


Fig. 3.12 Overall Displacements and deformations Panel 168-7 (H5)

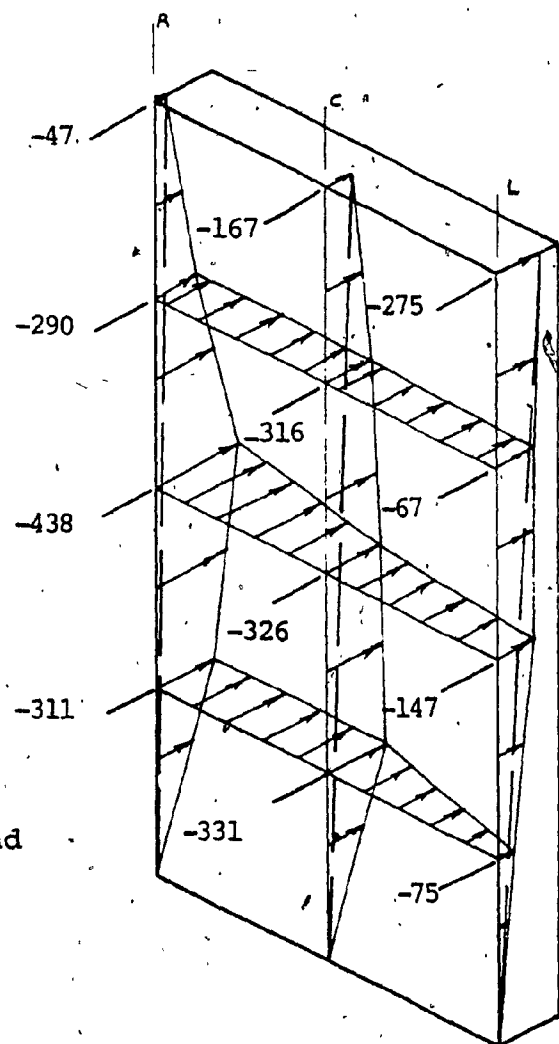


Fig. 3.13 Overall Displacements and deformation Panel 168-7 (H5).

Displacements  $\times 10^3$  (in)

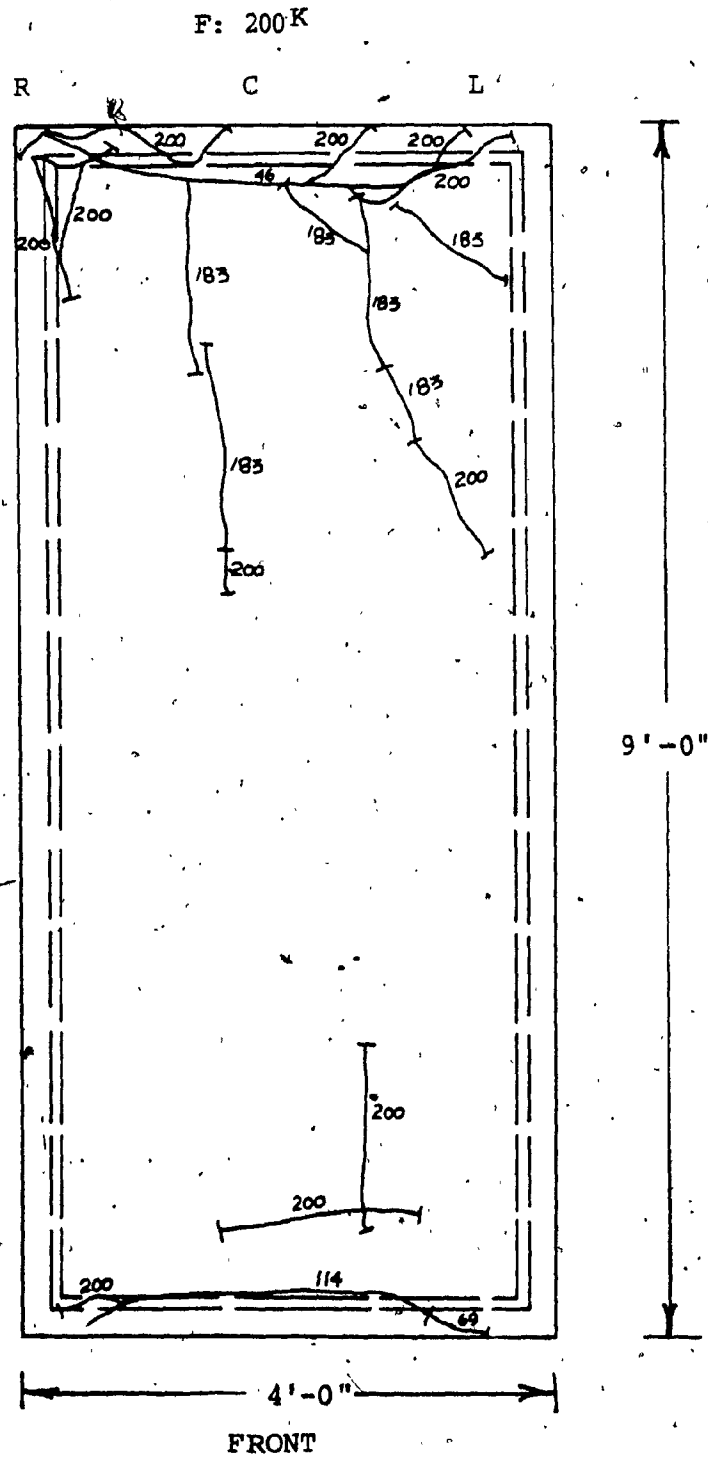
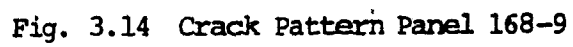


Fig. 3.14 Crack Pattern Panel 168-9

NOTE :Numbers correspond to loads in Kips





F: 226 K

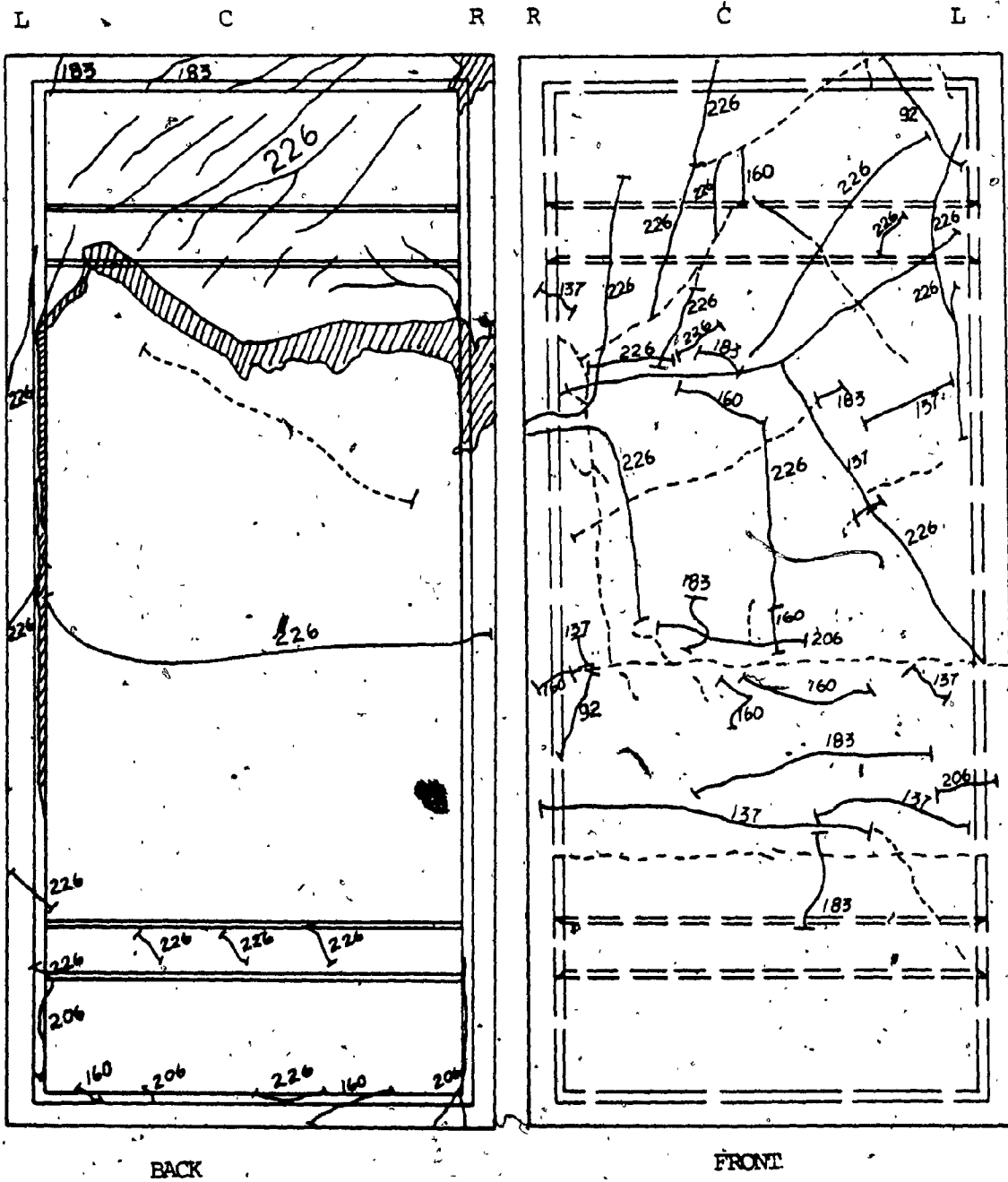


Fig. 3.15 Crack Pattern Panel 168-11 (H2)



F: 275 K

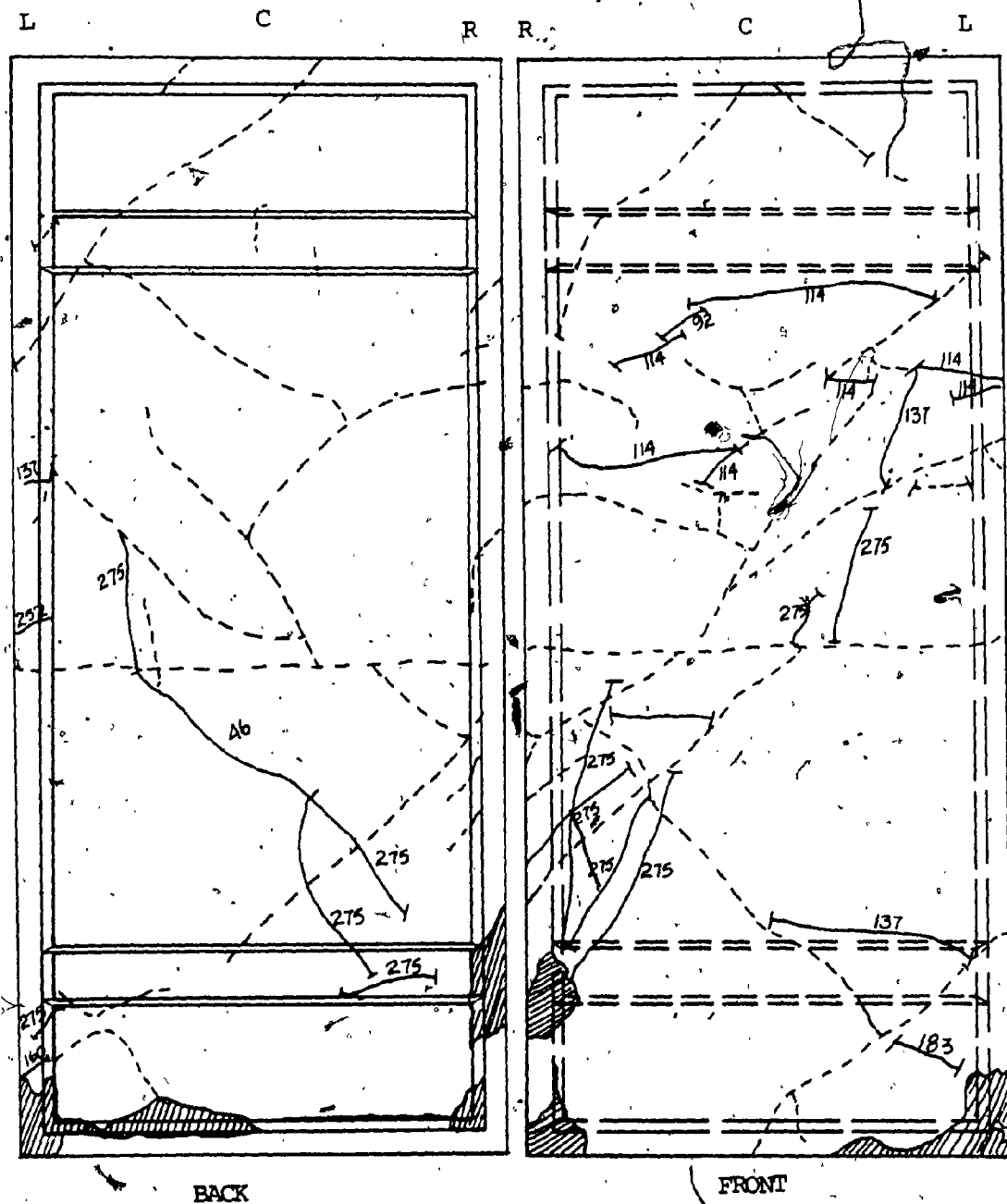


Fig. 3.17 Crack Pattern Panel 168-10 H4

F: 309K

L C R R C L

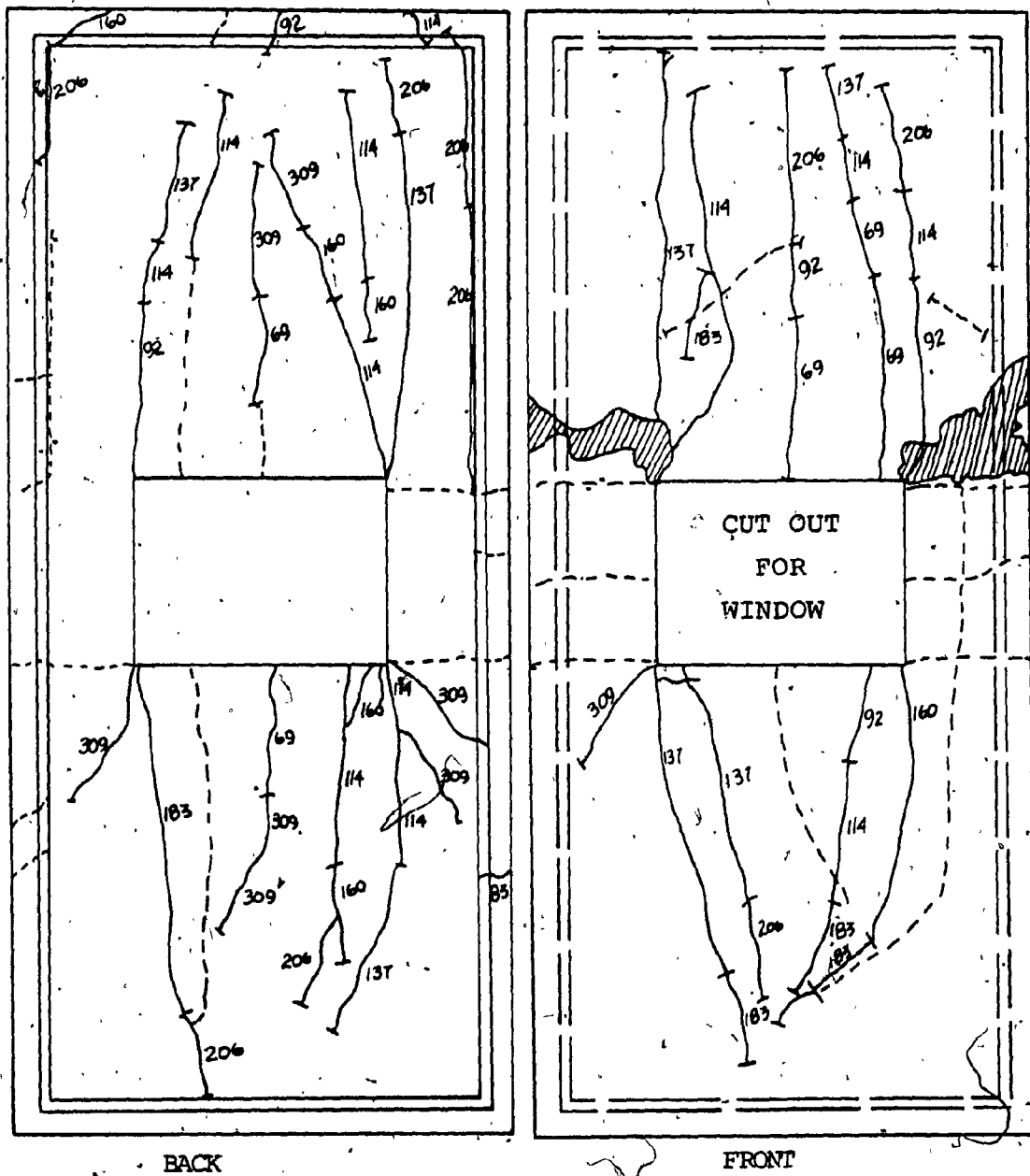


Fig. 3.18 Crack Pattern Panel 168-7 H5

CHAPTER 4

ANALYSIS OF TEST RESULTS

## ANALYSIS OF TEST RESULTS

### 4.1 Concentrically Loaded Panels

Since 1971 the "strength design method" adopted by ACI Building Code used the wall design equation [4.2], for the principal design procedure, allowing for the design of wall elements as columns, and defining "reasonably concentric loads" as those applied within the middle third of the cross section.

The equation was considered as a product of two functions.

$$\frac{P_u}{\phi f'_c b h} = F_1 \times F_2 \quad [4.1]$$

where  $F_1 = 0.55$ , and is function of eccentricity

$F_2 = [1 - (\frac{l_c}{40h})^2]$ , and is a function of slenderness.

Section 14.2.3 of the ACI 318-77 Building Code Requirements for Reinforced Concrete (7) expresses the wall design equation as:

$$P_u = 0.55 \phi A_g f'_c [1 - (\frac{l_c}{40h})^2] \quad [4.2]$$

It should be noted that equation [4.2] does not take into account the presence of steel. In the case of thin wall panels, because of smaller cross sectional area, contribution of steel may be more important and should

not be neglected. Thus, equation [4.2] was modified to take into account the presence of steel, given by:

$$P_u = 0.55 \phi A_g f'_c \left[ 1 - \left( \frac{l_c}{40h} \right)^2 \right] [1 + (m-1)p_m + (n-1)p_n] \quad [4.3]$$

where

- $P_u$  = factored vertical load on wall
- $f'_c$  = specified compressive strength of concrete
- $A_g$  = cross-sectional area.
- $l_c/h$  = height to thickness ratio of the wall
- $m$  =  $f_y/f'_c$  yield strength ratio of steel to concrete
- $p_m$  = ratio of yielded steel area to gross area
- $n$  =  $E_s/E_c$  modular ratio
- $p_n$  = ratio of non yielded steel area to gross area
- $\phi$  = capacity reduction factor.

The modified equation was used to calculate the carrying capacities of the concentrically loaded panels. In equation 4.3 the ratio of moduli of elasticity  $n$  for non yielded reinforcement and yield strength ratio  $m$  for yielded reinforcement will be assumed. The ratios were incorporated in the equation on the basis that maximum strain reached from concentrically loaded panels was 0.0016 in/in.



The computed values were compared to test results. The ratios of failure loads to computed carrying capacities, shown in table 4.1-2 result in ratios greater than the capacity reduction factor of 0.7 (recommended by ACI 318-77).

The carrying capacities of the panels were also calculated with direct application of equation 4.2, neglecting the presence of steel. The resulting capacity reduction factors, shown in table 4.1-2 are higher than values obtained with the modified equation. Thus, it may be noted, that the equation may be safely applied for the case of thin wall panels of properties comparable to those studied in this research. Detailed calculations are shown in Appendix A and B.

TABLE 4.1 COMPARISON OF FAILURE LOADS WITH CALCULATED  
VALUES FOR CONCENTRICALLY LOADED PANELS.

PANEL MARK	$P_u$ (Eqn. 4.5) KIPS	$P_u$ (Eqn. 4.2) KIPS	$P_f$ KIPS	$P_f/P_u = \phi$ (Eqn. 4.3)	$P_f/P_u = \phi$ (Eqn. 4.2)
168-11 H2	285	253	226	0.80	0.89
168-8 H3	282	265	270	0.96	1.02
168-10 H4	250	235	275	1.10	1.17
168-7 H5	294	251	309	1.06	1.23

#### 4.2 Eccentrically loaded Panels

Panel 168-9 marked as H1 failed at 200K. Due to its unsymmetrical shape, by placing the load on its geometric centre resulted in a small eccentricity. The carrying capacity of this panel was calculated considering the compatibility of strains of steel and concrete.

Because of small eccentricity the whole section was in compression, therefore contribution of steel was calculated on strain compatibility basis. The rib side was under maximum compression, hence it was assumed that extreme fibres reach ultimate strain of 0.003.

TABLE 4.2 Comparison of Failure loads with Calculated Values: Eccentrically loaded.

Panel MARK	$P_u$ KIPS	$P_f$ KIPS	$P_f/P_u = \phi$
168-9 H1	238	200	0.84

## CONCLUSIONS

From experimental and analytical results the following conclusions may be drawn.

(1) The design method for walls recommended by ACI (318-77) may be safely applied to the design of thin walled panels of comparable properties to panels studied. Such panels may have  $w/t \leq 32$  and an overall width to length ratio of  $h/l_c \leq 1/13.5$ . The method, using equation 14.1 of the ACI Code of Practice or the modified equation presented herein, is applicable to both axially loaded panels and panels having small structural eccentricity. In this case, eccentricity resulted since the center of gravity of the bearing foot did not coincide with the center of gravity of the panel itself.

(2) For panels tested, steel is significant and should be considered in the design practice.

(3) Panels which have a membrane on one side, deflect in the membrane direction. The displacements are larger in eccentrically loaded panels. Recorded displacements up to failure were relatively small in the range of  $h/247$  to  $h/331$ .

(4) First cracks which occurred on panels without cross ribs occurred at 114K to 137K loads. On panels without ribs, including the one with the cut out for window, cracks occurred at smaller loads of 46K and 69K. Under increasing load and increasing displacements in the direction of the

mebrane,existing centrally located shrinkage cracks were expanding.

(5) Generally all panels failed at the intersection of the membrane with edge ribs,except in the case of the panel with the window opening where failure occurred at window corners,where there were abrupt changes in cross section and concentration of stresses.Panels having cross ribs developed pronounced seperation from the wall membrane and failure occurred around ribs.

(6) The research reported,did not study the stability aspects of these panels. These formed the subject of other research carried out concurrently and results are presented in a separate paper (8).

(7) It should be noted here that conclusions given in this report are based on a limited number of model tests. There are other aspects influencing sterngth of thin wall panels which are not investigated and could be considered as a topic for further research.These include variation of reinforcement,influence of dimensional relationships and shape size and distribution of ribs.

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APPENDIX A

CONCENTRICALLY LOADED

PANELS: DESCRIPTION, MATERIALS, AREAS, STRENGTHS



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## APPENDIX A

### A.1 Panel, Description, Materials, Areas.

#### A.1.1 PANEL 168-11 (H2)

$$f'_c = 5073 \text{ psi}$$

$$A_g = 102.44 \text{ m}^2$$

$$I_c = 108 \text{ in.}$$

$$h = 8 \text{ in.}$$

#### Reinforcement

#### BARS

1#5	$f_y = 60 \text{ psi}$	$A_s = 0.31 \text{ in}^2$
1#8	$f_y = 60 \text{ psi}$	$A_s = 0.79 \text{ in}^2$
1#3	$f_y = 40 \text{ psi}$	$A_s = 0.11 \text{ in}^2$
1#4	$f_y = 40 \text{ psi}$	$A_s = 0.20 \text{ in}^2$

#### MESHES

6x6-10/10	$f_y = 83,449.9 \text{ psi}$	$A_s = 0.10 \text{ in}^2$
6x6-11	$f_y = 76,364.6 \text{ psi}$	$A_s = 0.44 \text{ in}^2$

#### A.1.2 PANEL 168-8 (H3)

$$f'_c = 5306$$

$$A_g = 102.44$$

$$I_c = 108 \text{ in.}$$

$$h = 8 \text{ in.}$$

#### Reinforcement

#### BARS

2#5	$f_y = 60 \text{ psi}$	$A_s = 0.62 \text{ in}^2$
1#2	$f_y = 40 \text{ psi}$	$A_s = 0.05 \text{ in}^2$
1#3	$f_y = 40 \text{ psi}$	$A_s = 0.11 \text{ in}^2$

#### MESHES

142-1220	$f_y = 85,314.7$	$A_s = 0.0715 \text{ in}^2$
6x6-6/6	$f_y = 72,884.2$	$A_s = 0.203 \text{ in}^2$

A.1.3. PANEL 168-10. (H4)

$$f'_c = 4698 \text{ psi}$$

SAME REINFORCEMENT AS PANEL 168-8

A.1.4 PANEL 168-7 (H5)

$$f'_c = 5023 \text{ psi}$$

$$A_g = 102.44$$

$$l_c = 108 \text{ in.}$$

$$h = 8"$$

Reinforcement

BARS

2#9	$f_y = 60 \text{ psi}$	$A_s = 2.0 \text{ in}^2$
1#3	$f_y = 40 \text{ psi}$	$A_s = 0.11 \text{ in}^2$
1#9	$f_y = 40 \text{ psi}$	$A_s = 0.20 \text{ in}^2$

MESHES

$$2-6 \times 6-6/6 \quad f_y = 72,884.3 \text{ psi} \quad A_s = 0.41 \text{ in}^2$$

## A.2 Panel Strengths (using equation 4.3)

In equation 4.3  $P_u$  is the design value used.  
 Since the ultimate  $P_u = P_u / \phi$ ,  $\phi$  may be evaluated from  
 ratio  $P_f / P_u$  where  $P_f$  is the failure load.

$$\phi = \frac{P_f}{P_u}$$

### A.2.1 Panel 168-11 (H2)

$$P_u = 0.55(5073)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right] \left[ 1 + \left( \frac{40,000 - 1}{5073} \right) \frac{0.31}{102.44} \right. \\ \left. + (7.07 - 1) \frac{1.64}{102.44} \right]$$

$$P_u = 283K, \quad \bar{P}_u = 283 \phi$$

$$P_f = 226K$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{226}{283}$$

$$\phi = 0.80$$

### A.2.2 Panel 168-8 (H3)

$$P_u = 0.55(5306)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right] \left[ 1 + \left( \frac{40,000 - 1}{5306} \right) \frac{0.16}{102.44} \right. \\ \left. + (6.91 - 1) \frac{0.895}{102.44} \right]$$

$$P_u = 281K, \quad \bar{P}_u = 281 \phi$$

$$P = 270K$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{270}{281}$$

$$\phi = 0.96$$

A.2.3 Panel 168-9 (H4)

$$P_u = 0.55(4698)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right] \left[ 1 + \left( \frac{40.00}{4698} - 1 \right) \frac{0.16}{102.44} \right. \\ \left. + (7.34 - 1) \frac{0.895}{102.44} \right]$$

$$P_u = 250 \text{ K} ; \bar{P}_u = 250 \text{ } \phi$$

$$P_f = 275 \text{ K}$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{275}{250}$$

$$\phi = 1.10$$

A.2.4 Panel 168-7 (H5)

$$P_u = 0.55(5023)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right] \left[ 1 + \left( \frac{40,000}{5023} - 1 \right) \frac{0.31}{102.44} \right. \\ \left. + (7.10 - 1) \frac{2.41}{102.44} \right]$$

$$P_u = 292 \text{ K} ; \bar{P}_u = 292 \text{ } \phi$$

$$P_f = 309 \text{ K}$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{309}{292}$$

$$\phi = 1.06$$

A.3 Panel Strengths (using equation 4.2)

Using Eqn 4.2 which neglects the presence of steel the capacity reduction factor is evaluated by calculating

$P_u$ . Since  $\bar{P}_u = \frac{P_u}{\phi}$

$$\phi = P_f / P_u$$

A.3.1 Panel 168-11 (H2)

$$P_u = 0.55(5073)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right]$$

$$P_u = 253 \text{ K}; \bar{P}_u = 253 \phi$$

$$P_f = 226 \text{ K}$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{226}{253}$$

$$\therefore \phi = 0.89$$

A.3.2 Panel 168-8 (H3)

$$P_u = 0.55(5306)(102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right]$$

$$P_u = 265 \text{ K}; \bar{P}_u = 265 \phi$$

$$P_u = 270 \text{ K}$$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{270}{265}$$

$$\therefore \phi = 1.02$$

A.3.3 Panel 168-9 (H4)

$$P_u = 0.55 (4698) (102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right]$$

$$P_u = 235K ; \bar{P}_u = 235 \phi$$

$$P_u = 275K$$

$$\phi = P_f / \bar{P}_u = \frac{275}{235}$$

$$\phi = 1.17$$

A.3.4. Panel 168-7 (H5)

$$P_u = 0.55 (5023) (102.44) \left[ 1 - \left( \frac{108}{40 \times 8} \right)^2 \right]$$

$$P_u = 257K ; \bar{P}_u = \frac{251}{\phi}$$

$$P_u = 309K$$

$$\phi = P_f / \bar{P}_u = \frac{309}{251}$$

$$\phi = 1.23$$

APPENDIX B

ECCENTRICALLY LOADED

PANEL: DESCRIPTION, MATERIALS, AREAS & STRENGTH

## APPENDIX B

### B.1 Panel Description, Materials, Areas

#### B.1.1 Panel 168-9 (H1)

$$\begin{aligned} f'_c &= 5269 \text{ psi} \\ A_g &= 102.44 \text{ in}^2 \\ l_c &= 108 \text{ in.} \\ h &= 8 \text{ in.} \end{aligned}$$

#### Reinforcement

#### BARS

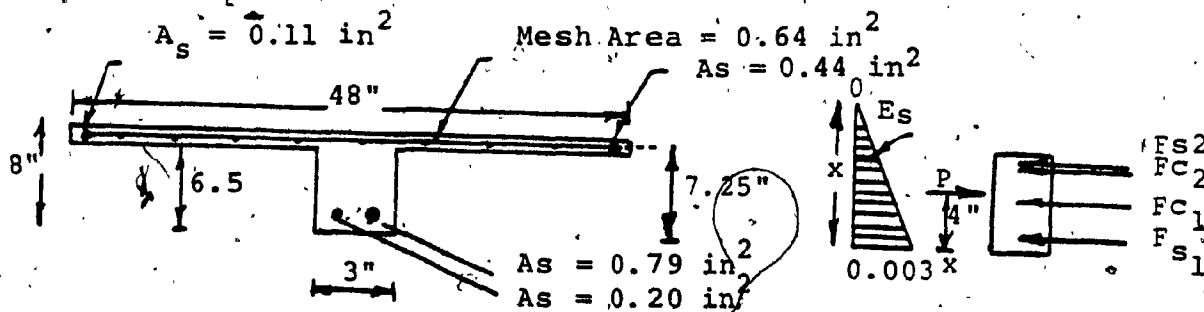
1#3	$f_y = 40,000$	$A_s = 0.11 \text{ in}^2$
1#4	$f_y = 40,000$	$A_s = 0.20 \text{ in}^2$
1#6	$f_y = 40,000$	$A_s = 0.44 \text{ in}^2$
1#8	$f_y = 60,000$	$A_s = 0.79 \text{ in}^2$

#### MESHES

6x6-1/1	$f_y = 76,364.6 \text{ psi}$	$A_s = 0.44 \text{ in}^2$
6x6-6/6	$f_y = 72,884.3 \text{ psi}$	$A_s = 0.20 \text{ in}^2$

### B.2 Panel Strength

#### Equivalent Section



$$B_1 = 0.787$$

$$a = 0.787 x$$

$$\epsilon_s / 0.003 = \frac{x - 7.25}{x}$$

$$F_{s2} = \epsilon_s \cdot A_s \cdot E_s$$



$$F_{c1} = 0.85 f'_c a_1 b_1$$

$$F_{c2} = 0.85 f'_c a_2 b_2$$

$$F_{s1} = A_{s1} f_{y1} + A_{s2} f_{y2}$$

$$F_{s2} = \epsilon_s E_s A_s$$

$$F_{c1} = 0.85(5259)(6)(0.787(x-6.5)) \quad \therefore F_{c2} = 147.76x - 1220.35 \text{ kip}$$

$$F_{c2} = 0.85(5.259)(42)(0.787-6.5)$$

$$F_{c2} = 147.76x - 1220.35 \text{ kip}$$

$$F_{s1} = 0.20(40) + 0.79(60)$$

$$F_{s1} = 55.40 \text{ kip}$$

$$F_{s2} = 0.003 \times 1.193 \times 29 \times 10^3 \left[ \frac{x-7.25}{x} \right]$$

$$F_{s2} = 103.79 \left[ \frac{x-7.5}{x} \right] \text{ kip}$$

$$\sum M_o = 0$$

$$P(x-4) = F_{s2}(x-7.25) + F_{s1}(x-0.75) + F_{c1} \left( \frac{-0.787x}{2} \right)$$

$$+ F_{c2} \left( \frac{x-(0.78x-6.5)}{2} \right)$$

$$P(x-4) = 103.79 \left( \frac{x-7.25}{x} \right)^2 + 55.40(x-0.75) + 21.11 x \left( \frac{x-0.78x}{2} \right)$$

$$+ 147.76x - 1220.35 \left( \frac{-0.787x+6.5}{2} \right)$$

$$P(x-4) = 28.54x^2 + 509.44 x + \frac{5455.25}{x} - 5512.66$$

$$(x-4)$$

[B-1]

$$\sum F = 0$$

$$P = 21.11x + (147.76x - 1220.35) + 55.40 + 103.79 \left[ \frac{x-7.25}{x} \right]$$

$$P = 168.87x - 1061.16 - \frac{752.48}{x}$$

[B-2]

Equating [B-1] & [B-2] yields the following equation.

$$140.33x^3 - 2246.04x^2 + 9004.82x - 2445.34 = 0$$

[B-3]

Solving the above equation:

$$x = 9.322"$$

Since  $a = 0.787 x$

$$a = 0.787 (9.323)$$

$$a = 7.337"$$

∴ 'a' falls in the slab.

from eq <sup>n</sup> [B-2] ; substituting for x:

$$P = 168.87(9.323) - 1061.16 - \frac{752.48}{9.323}$$

$$P = 432.50 K$$

Multiplying the above  $P$  by a factor of 0.55 to take into consideration eccentricity;

$$P_u = 0.55 P$$

$$= 0.55 (432.50)$$

$$P_u = 238 K$$

Since  $\bar{P}_u = \frac{P_u}{\phi}$  and  $P_f = 200^k$

$$\phi = \frac{P_f}{\bar{P}_u} = \frac{200}{238}$$

$$\phi = 0.84$$

APPENDIX C  
TEST PANEL PHOTOGRAPHS



Figure C1  
Loading Scheme



Figure C2  
Overall View of the  
Loading Scheme

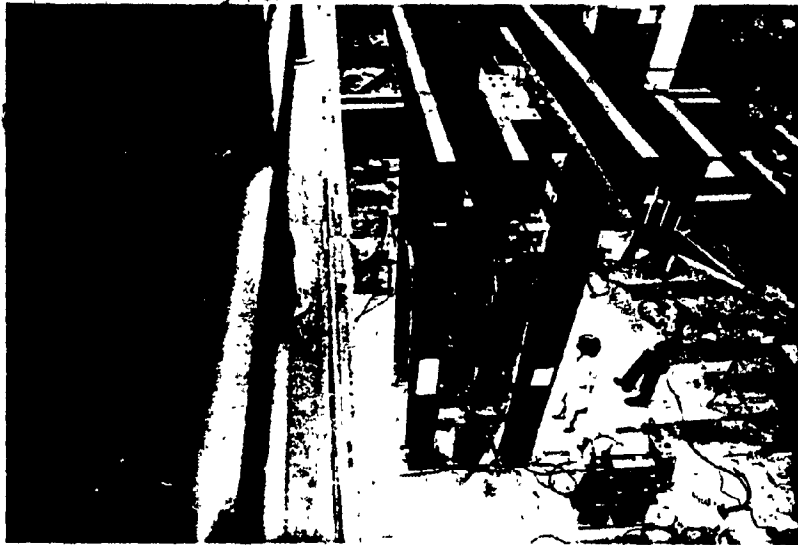


Figure C3  
Overall View of the Loading Frame

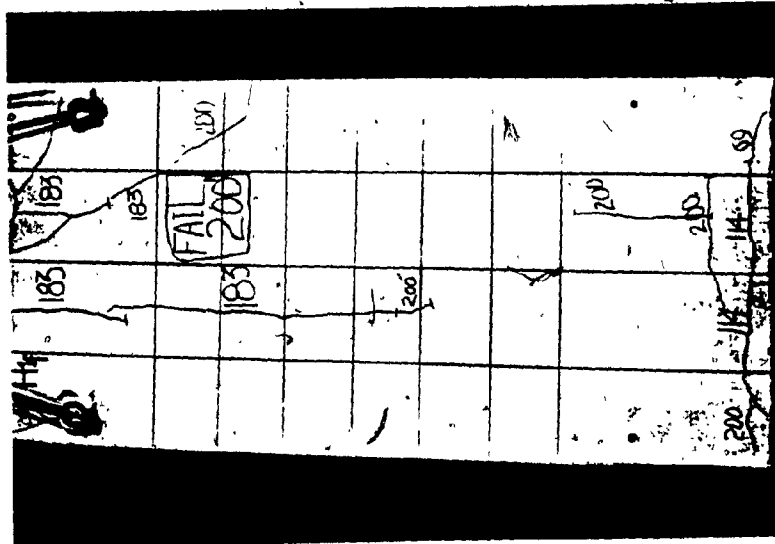


Figure C5  
Front View of Panel 168-9 (H1)  
(At Failure)

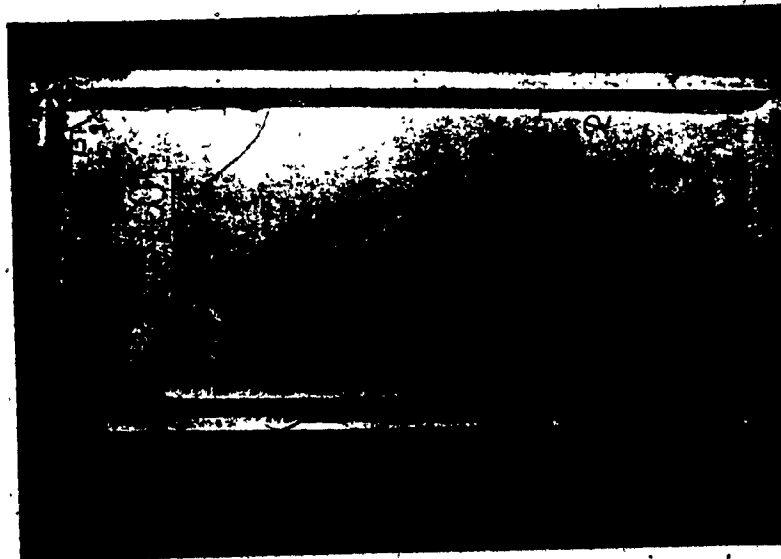


Figure C4  
Back View of Panel 168-9 (H1)  
(At Failure)

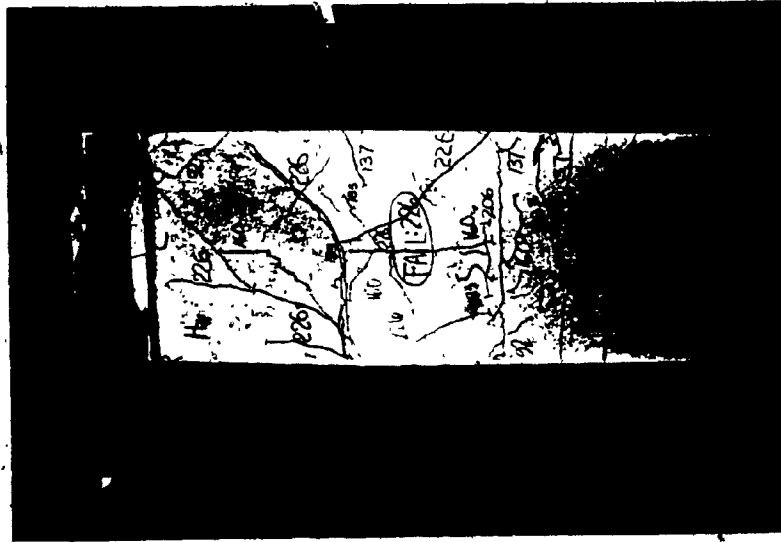


Figure C7  
Front View of Panel 168-11 (H2)  
(At Failure)

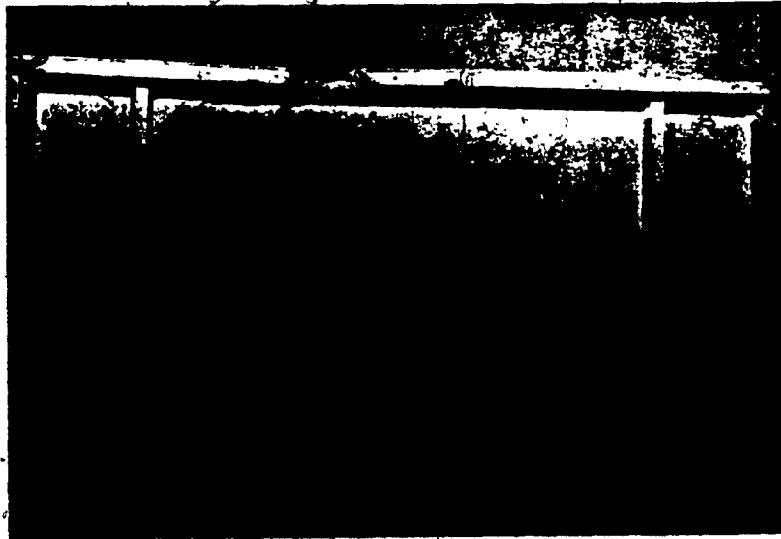


Figure C6  
Back View of Panel 168-11 (H2)  
(At Failure)



Figure C8  
View of Panel 168-11 (H2) in Test Frame  
(At Failure)



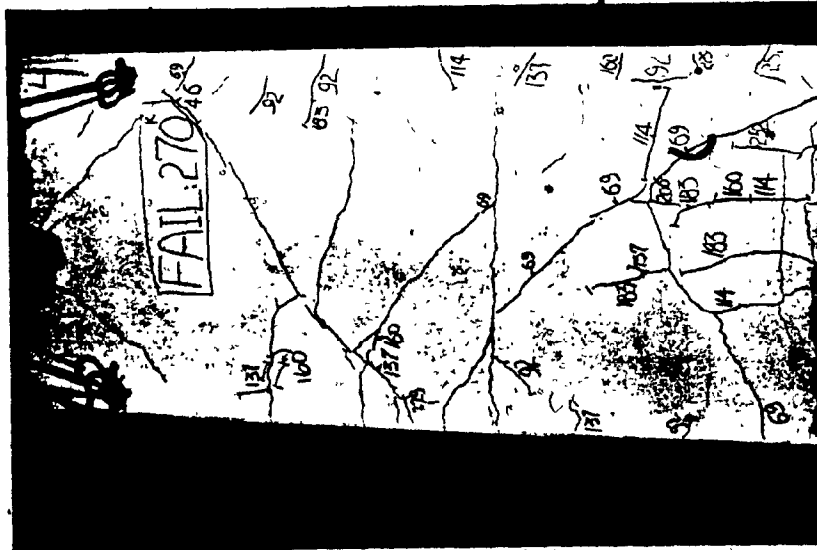


Figure C10  
Front View of Panel 168-8 (H3)  
(At Failure)

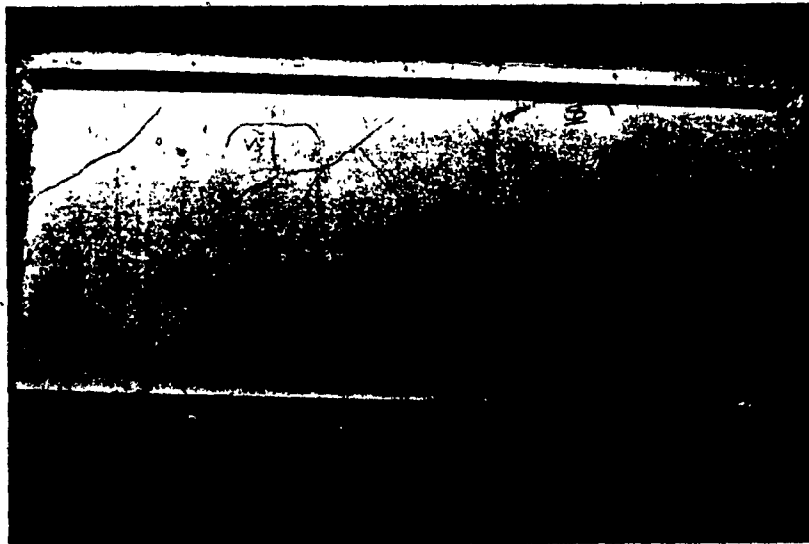


Figure C9  
Back View of Panel 168-8 (H3)  
(At Failure)

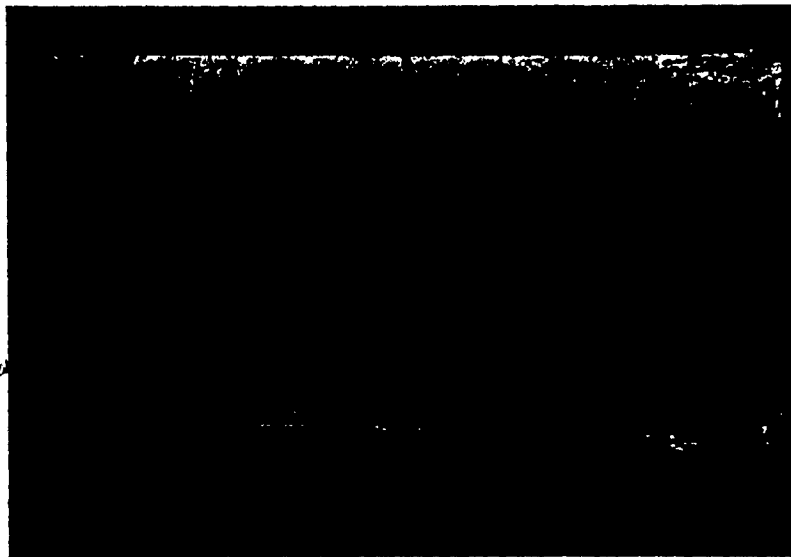


Figure C12  
Front View of Panel 168-10 (H4)  
(At Failure)

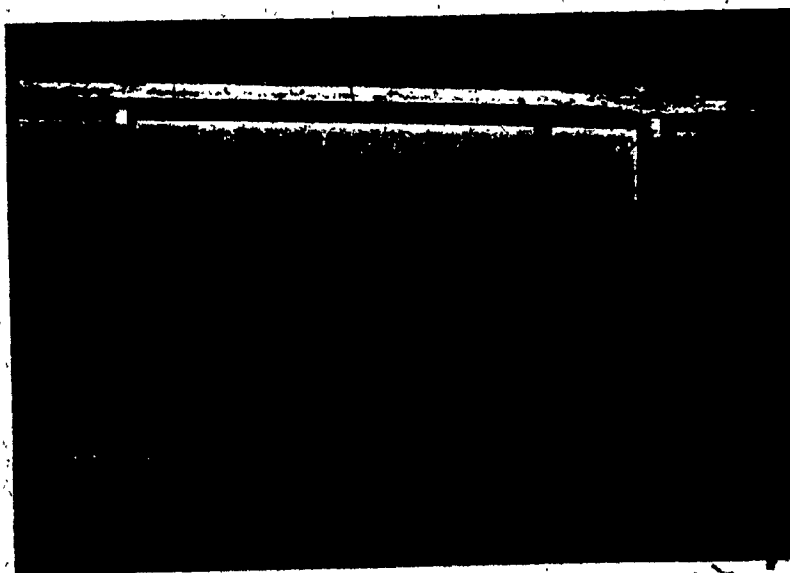


Figure C11  
Back View of Panel 168-10 (H4)  
(At Failure)

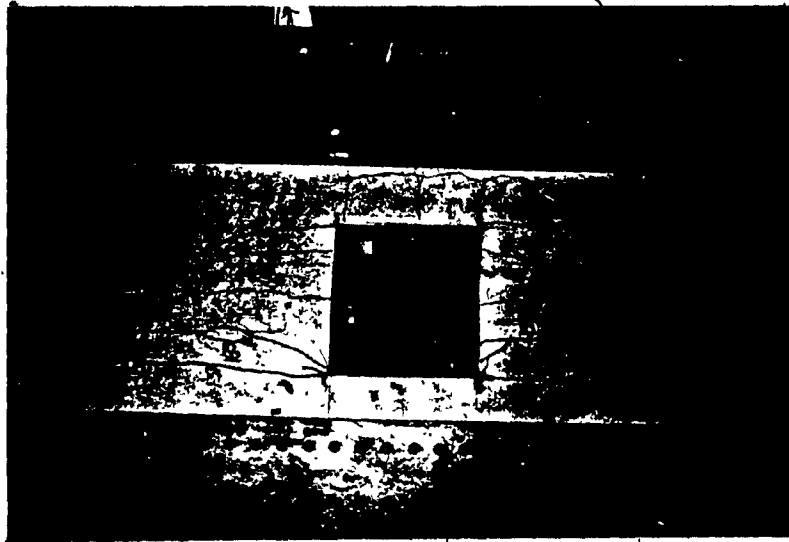


Figure C14  
Front View of Panel 168-7 (H5)  
(At Failure)

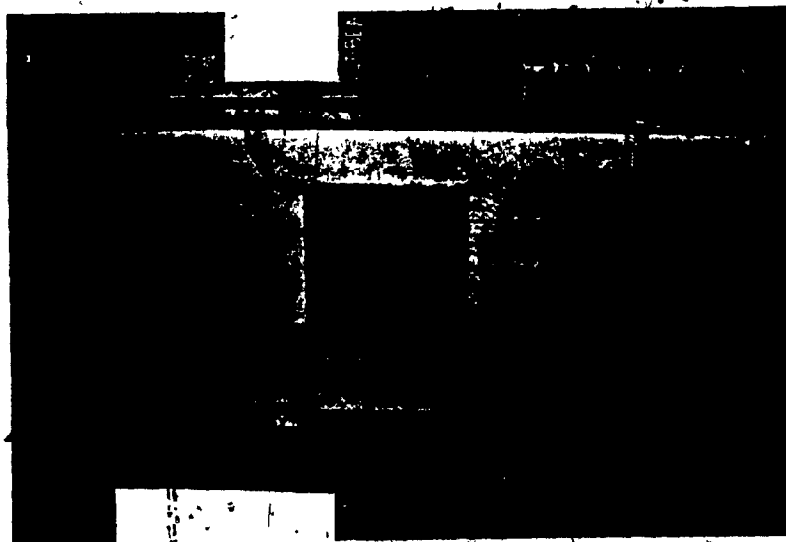


Figure C13  
Back View of Panel 168-7 (H5)  
(At Failure)